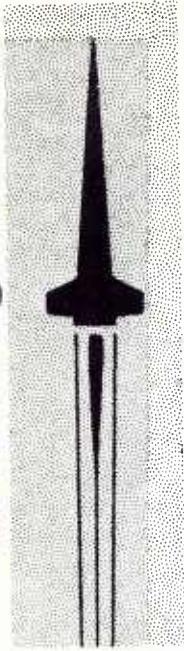


## UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER TD-CR-77-2	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) MCARLO: A COMPUTER PROGRAM FOR GENERATING MONTE-CARLO TRAJECTORIES IN A TIME-VARYING MAN/MACHINE CONTROL TASK		5. TYPE OF REPORT & PERIOD COVERED Contractor Report
		6. PERFORMING ORG. REPORT NUMBER 3463
7. AUTHOR(s)  David L. Kleinman, Sheldon Baron, and Jeffrey E. Berliner		8. CONTRACT OR GRANT NUMBER(s)  DAAH01-76-C-0194
9. PERFORMING ORGANIZATION NAME AND ADDRESS Bolt Beranek and Newman Inc. 50 Moulton Street Cambridge, Massachusetts 02138		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS
11. CONTROLLING OFFICE NAME AND ADDRESS Commander, US Army Missile R&D Command ATTN: DRDMI-TI Redstone Arsenal, AL 35809		12. REPORT DATE 10 Jun 1977
		13. NUMBER OF PAGES 105
14. MONITORING AGENCY NAME & ADDRESS (If different from Controlling Office) Commander, US Army Missile R&D Command ATTN: DRDMI-TD Redstone Arsenal, AL 35809		15. SECURITY CLASS. (of this report)  UNCLASSIFIED
		15a. DECLASSIFICATION/DOWNGRADING SCHEDULE
16. DISTRIBUTION STATEMENT (of this Report)  Approved for public release; distribution unlimited.		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) MCARLO Fortran TIVAR		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number)  MCARLO is a computer program for generating time histories of pertinent variables in a man-machine control task. The optimal control model forms the basis for the Monte-Carlo simulation equations. This report gives the modeling formulation and requisite discretization of the equations, a description of the MCARLO subroutines, and input deck setup and a sample problem with solution.		

ADA045037



**U.S. ARMY  
MISSILE  
RESEARCH  
AND  
DEVELOPMENT  
COMMAND**



Redstone Arsenal, Alabama 35809



**TECHNICAL REPORT TD-CR-77-2**

**MCARLO: A COMPUTER PROGRAM FOR GENERATING  
MONTE-CARLO TRAJECTORIES IN A TIME-VARYING  
MAN/MACHINE CONTROL TASK**

Bolt Beranek and Newman Inc.  
50 Moulton Street  
Cambridge, Massachusetts 02138

10 June 1977



APPROVED FOR PUBLIC RELEASE; DISTRIBUTION UNLIMITED

*Prepared for:*  
Aeroballistics Directorate  
Technology Laboratory

#### **DISPOSITION INSTRUCTIONS**

**DESTROY THIS REPORT WHEN IT IS NO LONGER NEEDED. DO NOT  
RETURN IT TO THE ORIGINATOR.**

#### **DISCLAIMER**

**THE FINDINGS IN THIS REPORT ARE NOT TO BE CONSTRUED AS AN  
OFFICIAL DEPARTMENT OF THE ARMY POSITION UNLESS SO DESIG-  
NATED BY OTHER AUTHORIZED DOCUMENTS.**

#### **TRADE NAMES**

**USE OF TRADE NAMES OR MANUFACTURERS IN THIS REPORT DOES  
NOT CONSTITUTE AN OFFICIAL INDORSEMENT OR APPROVAL OF  
THE USE OF SUCH COMMERCIAL HARDWARE OR SOFTWARE.**

## TABLE OF CONTENTS

<u>Section</u>	<u>Page</u>
1. COMPUTER PROGRAM ABSTRACT . . . . .	1
2. PROBLEM FORMULATION AND ALGORITHMS . . . . .	2
2.1 System-Display Dynamics . . . . .	2
2.2 Human Operator Internal Model . . . . .	4
2.3 Human Limitations . . . . .	5
2.4 Discretized Equations . . . . .	7
2.5 Human Operator Model Equations . . . . .	9
2.6 Special Considerations . . . . .	11
2.7 Summary of Human Model Computations . . . . .	12
3. PROGRAM DESCRIPTION . . . . .	14
3.1 MAIN Program . . . . .	14
3.2 Subroutine SYSTM . . . . .	14
3.3 Subroutine UPDATE . . . . .	16
3.4 Subroutine MAN . . . . .	17
3.5 Subroutine INFORM . . . . .	17
3.6 Subroutine PRINTR . . . . .	18
3.7 Program Operation . . . . .	18
4. INPUT DECK SETUP . . . . .	19
4.1 Control Cards . . . . .	19
4.2 System Parameter Cards . . . . .	20
4.3 Man-Model Parameter Cards . . . . .	22
4.4 Entering Parameter Data . . . . .	24
4.5 User Written Routines . . . . .	24
5. SAMPLE PROBLEM . . . . .	25
5.1 Sample Problem Description . . . . .	25
5.2 User Written Subroutines for the Sample Problem . . . . .	28

5.3	Input deck for the Sample Problem . . . . .	29
5.4	Output listing for the Sample Problem . . . . .	30
6.	COMMON BLOCK USAGE . . . . .	47
7.	MCARLO LISTING . . . . .	49

## 1. COMPUTER PROGRAM ABSTRACT

PROGRAM NAME: MCARLO

ORIGINATOR: Bolt Beranek and Newman Inc.  
50 Moulton Street  
Cambridge, Massachusetts 02138  
(617) 491-1850  
David L. Kleinman, Sheldon Baron,  
and Jeffrey E. Berliner

CONTRACT MONITOR: U. S. Army Missile Command  
Aeroballistics Directorate  
(205) 876-1951  
Richard E. Dickson

CONTRACT NUMBER: DAAH01-76-C-0194

## PROGRAM ABSTRACT

MCARLO is a computer program for generating simulated time histories of pertinent variables in a man-machine control task. The optimal control model (OCM) forms the basis for the Monte-Carlo simulation equations. The ensemble statistics of such time functions must agree with the covariance propagation results obtained via more direct methods, e.g., using TIVAR.

The MCARLO program is written in the FORTRAN-IV-EXTENDED computer programming language, and is designed for efficient batch operation on a Control Data CDC-6600 computer. Data input to the program is provided on standard punched cards and output is generated via the lineprinter.

In this manual we give the modeling formulation and requisite discretization of the equations, a description of the MCARLO subroutines, the input deck setup and a sample problem with solution.

## 2. PROBLEM FORMULATION AND ALGORITHMS

The major aspects of computer simulation for a man-machine system are shown in Figure 1. The modeling issues are discussed below.

### 2.1 System-Display Dynamics

There are no modeling restrictions on the system being controlled, other than the generation of a set of NY displayed elements  $y_t$  at time t from:

$u(t)$  = human's control inputs, NU vector

$w(t)$  = random input disturbances, NW vector

$z(t)$  = "deterministic" inputs, NZ vector.

In its most general mathematical form, the system/display dynamics might be modeled by:

$$\dot{x}(t) = f(t, x(t), u(t), w(t), z(t)); \quad x_0 = x(t_0) \quad (1)$$

$$y(t) = h(t, x(t), u(t)) \quad (2)$$

where  $x(t)$  = NX system state vector. The vector  $w(t)$  consists of independent zero mean white Gaussian noise inputs with covariance

$$E[w_i(t) w_j(\sigma)] = W_{Sij}^0(t) \delta(t-\sigma) \quad i=1, \dots, NW \quad (3)$$

For the special case of a linear time-varying system, the equations (1)-(2) become:

$$\dot{x}(t) = A_s x(t) + B_s u(t) + E_s w(t) + F_s z(t) \quad (4)$$

$$y(t) = C_s x(t) + D_s u(t) \quad (5)$$

The system parameters, which may be time varying, are:

$A_s$  = NX by NX state matrix

$B_s$  = NX by NU control matrix

$E_s$  = NX by NW noise matrix

$F_s$  = NX by NZ bias input matrix

$C_s$  = NY by NX state display matrix

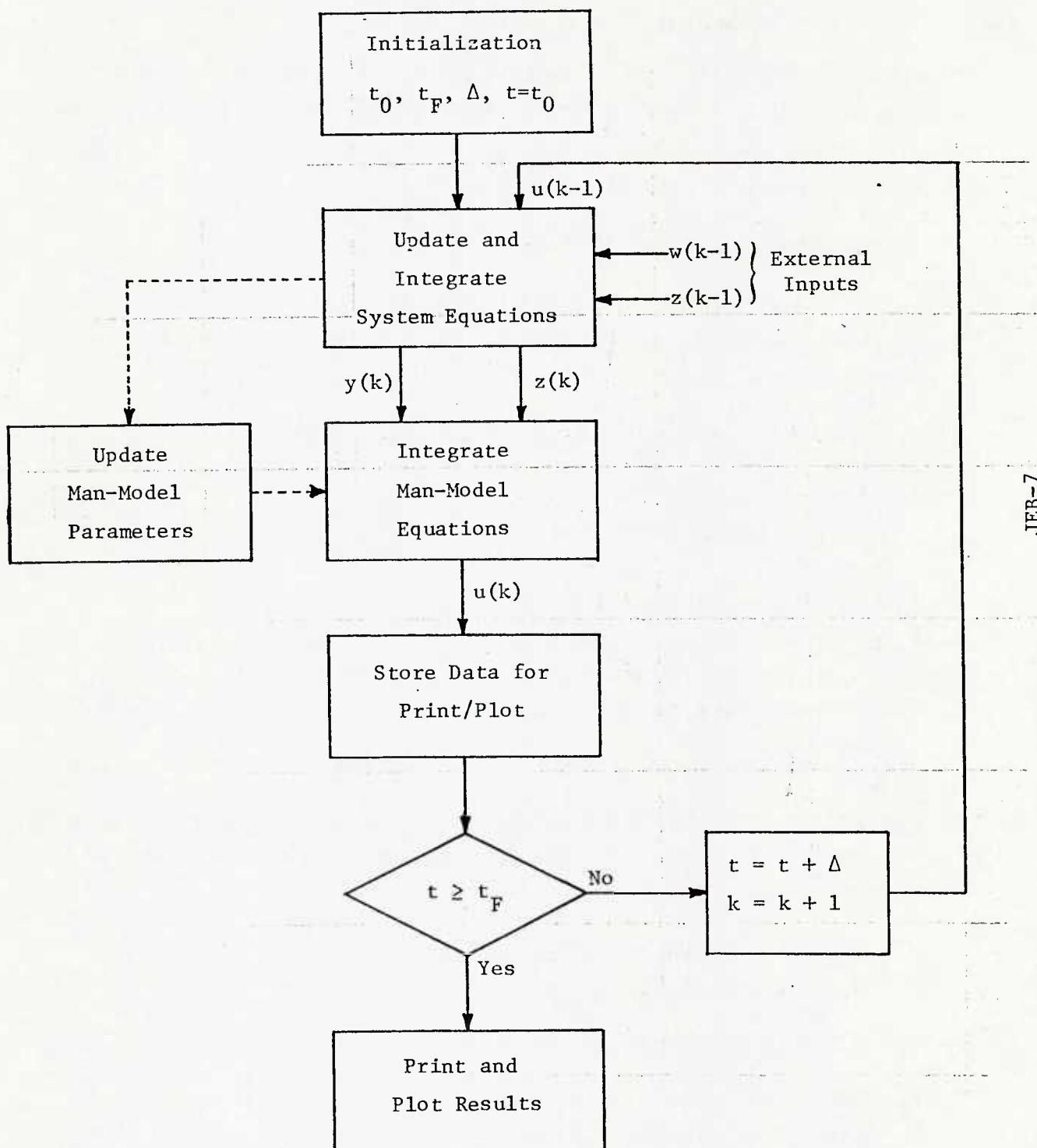


Figure 1. Major Aspects of Computer Simulation for a Man-Machine System

$D_s$  = NY by NU control display matrix

A means for updating the system parameters, as a function of time, must be included along with the system description. Since the form of updating is highly dependent upon the system model, a general updating scheme is feasible for only the highly structured linear case.

## 2.2 Human Operator Internal Model

In the OCM, the human is assumed to have an internal characterization of the input-output response of the system. This "internal model" is assumed to be linear, in state variable form,

$$\dot{x}_m(t) = A_m x_m(t) + B_m u_m(t) + E_m w_m(t) + F_m z_m(t) \quad (6)$$

$$y_m(t) = C_m x_m(t) + D_m u_m(t) \quad (7)$$

where

$x_m(t)$  = internal model states, NXM vector

$z_m(t)$  = model deterministic inputs, NZM vector

(present formulation requires  $z_m = z$  so NZM=NZ)

$w_m(t)$  = model Gaussian white noise inputs, NWM vector

$$E[w_{mi}(t) w_{mi}(\sigma)] = W_{mi}^0(t) \delta(t-\sigma); \quad i=1, \dots, NWM \quad (8)$$

The model inputs  $u_m(t)$  and displayed outputs  $y_m(t)$  are assumed to be the same as the actual system inputs  $u(t)$  and displays  $y(t)$  to avoid numerous conceptual problems. Thus,

$$u_m(t) = u(t) \text{ and NUM} = NU$$

$$y_m(t) = y(t) \text{ and NYM} = NY.$$

The internal model parameters, which can be time-varying, are:

$A_m$  = NXM by NXM model state matrix

$B_m$  = NXM by NUM model control matrix

$E_m$  = NXM by NWM model noise matrix

$F_m$  = NXM by NZM model bias input matrix

$C_m$  = NYM by NXM model output matrix for states

$D_m$  = NYM by NUM model output matrix for controls

The choice of model parameter matrices is somewhat subjective. In the general non-linear case, these matrices typically would approximate the partial derivatives of  $f$  and  $h$  in Equations (1)-(2), i.e.,

$$A_m \approx \frac{\partial f}{\partial X}, \text{ etc.}$$

In the linear system case of Equations (4)-(5), the model typically would reflect an appropriate lower order characterization of the true system dynamics. Of course, a not unreasonable choice for the model matrices is:

$$A_m = A_s, \text{ etc.}$$

Here, the model parameter is assumed to be same as the associated system parameter. This is a convenient assumption as it greatly simplifies the process of updating model matrices for time varying systems.

The internal model is used within the OCM to help generate a (continuous time) human operator control input via:

$$\dot{u}(t) = -L_c \begin{bmatrix} \hat{x}_m(t) \\ u(t) \end{bmatrix} + L_{c2} v_u(t) \quad . \quad (9)$$

The NUM by (NXM+NUM) feedback gains

$$L_c = [T_N^{-1} L_{opt} \mid T_N^{-1}] = [L_{c1} \mid L_{c2}] \quad (10)$$

are generated via auxiliary programs that solve the optimal control problem for the model equations. The model is also needed in the construction of the Kalman filter-predictor that generates the model state estimate  $\hat{x}_m(t)$ .

### 2.3 Human Limitations

The human generates  $\hat{x}_m(t)$  on the basis of the delayed and noisy perceived information:

$$y_{pi}(t) = N_i[y_i(t-\tau)] + v_{yi}(t) \quad i=1, \dots, NY \quad (11)$$

where

$\tau$  = the human's time delay,

$v_y(t)$  = the observation or sensor noise at time  $t$ ,

and  $N_i(\cdot)$  is the non-linear observation threshold:

$$N_i(x) = \begin{cases} x - a_i & x > a_i \\ 0 & |x| \leq a_i \\ x + a_i & x < -a_i \end{cases} \quad (12)$$

In a simulation model, it is possible to implement the non-linear observations using Equations (11) and (12). However, in a man-machine context we find it more convenient to replace  $N_i(\cdot)$  by an equivalent gain,  $\hat{N}_i$ . The random input describing function:

$$\hat{N}_i = \operatorname{erfc} \frac{|x|}{a_i \sqrt{2}} \quad (13)$$

is used.  $N_i$  is interpreted as the probability that the human will respond to  $y_i$ , given its present value at time  $t$ .

Each sensor noise  $v_{y_i}(t)$  is a zero-mean, white Gaussian noise with covariance:

$$E[v_{y_i}(t) v_{y_i}(\sigma)] = \frac{v_{y_i}^o(t)}{f_i(t)} \delta(t-\sigma) \quad (14)$$

that contains both an additive and a ratioed component:

$$v_{y_i}^o(t) = v_{y_i}(t) + \pi \rho_{y_i} E[y_i^2(t-)] \quad (15)$$

The quantity  $f_i > 0$  is the attentional allocation to the displayed variable  $y_i$ . The  $f_i$  are constrained by:

$$\frac{1}{2} \sum_{i=1}^{NY} f_i(t) = f_T = \text{constant total attention} \quad (16a)$$

$$f_{i+1}(t) = f_i(t) \quad i=1, 3, \dots, NY-1 \quad (16b)$$

to indicate that position-velocity pairs are obtained simultaneously from the display elements.

The neuro-motor interface portion of the model is given by Equation (9). The motor noises  $v_{ui}(t)$ ,  $i=1, \dots, NU$  are zero-mean white Gaussian, with covariance:

$$E[v_{ui}(t) v_{ui}(\sigma)] = V_{ui}^0(t) \delta(t-\sigma) \quad (17)$$

that contains an additive and a ratioed component,

$$V_{ui}^0(t) = v_{ui}(t) + \pi \rho_{ui} \text{Var}[u_i(t)] \quad (18)$$

## 2.4 Discretized Equations

The implementation of the human operator simulation on a digital computer requires the discretization of both system and model equations.

Given a computer time step  $\Delta$ , the system must generate  $y(k) \equiv y(t_0+k\Delta) = y(t)$  from the inputs  $u(k-1)$ ,  $w(k-1)$ , and  $z(k-1)$  which are assumed to be piecewise-constant over the previous time interval, e.g.,

$$u(t) = u(k-1) \quad t_0+(k-1)\Delta < t \leq t_0+k\Delta \quad (19)$$

For the case in which the system is described by the linear equations (4)-(5), the discretization chosen is:

$$x(k+1) = \Phi_s x(k) + \Gamma_s u(k) + \Delta [E_s w(k) + F_s z(k)] \quad (20)$$

$$y(k) = C_s x(k) + D_s u(k-1) \quad (21)$$

where  $x(0) = x(t_0)$  = initial state. The discrete system matrices  $\Phi_s$  and  $\Gamma_s$  are:

$$\Phi_s = e^{As\Delta} ; \quad \Gamma_s = \int_0^\Delta e^{As\sigma} B_s d\sigma \quad (22)$$

Discretization of the linear model equations (6)-(7) is done in a manner similar to the above. Thus

$$x_m(k+1) = \Phi_m x_m(k) + \Gamma_m u(k) + \Delta [E_m w_m + F_m z_m(k)] \quad (23)$$

$$y(k) = C_m x_m(k) + D_m u(k-1) \quad (24)$$

where

$$\Phi_m = e^{A_m \Delta} ; \quad \Gamma_m = \int_0^{\Delta} e^{A_m \sigma} B_m d\sigma \quad (25)$$

The human operator model must generate a control input  $u(k)$ , to use over the time interval  $(t, t+\Delta)$ , via

$$\frac{u(k) - u(k-1)}{\Delta} = -L \begin{bmatrix} \hat{x}_m(k) \\ u(k-1) \end{bmatrix} + L_2 v_u(k) \quad (26)$$

Note that it is the control input itself that is considered to be piecewise constant for interface with the system model. This is in contrast to the covariance propagation approach where control-rate is assumed piecewise constant with:

$$\dot{u}(k) = -L_d \begin{bmatrix} \hat{x}(k) \\ u(k) \end{bmatrix} + L_{d2} v_u(k) \quad (27)$$

The gains  $L = [L_1 \ L_2]$  in Equation (26) are computed from either the gains  $L_d$  or  $L_c$  according to

$$L = \frac{1}{2} L_d \quad (28a)$$

or

$$L = \frac{1}{2} \hat{L}_d \quad (28b)$$

respectively, where  $\hat{L}_d$  are the equivalent discrete gains:

$$\begin{aligned} \hat{L}_d &= L_c \left[ \frac{1}{\delta} \int_0^\delta e^{-\bar{A}\sigma} d\sigma \right] \\ \bar{A} &= \begin{bmatrix} A_m & B_m \\ -L_{c1} & -L_{c2} \end{bmatrix} \end{aligned} \quad (29)$$

The discretized observations are:

$$y_{pi}(k) = \hat{N}_i y_i(k-N) + v_{yi}(k) \quad (30)$$

where  $N = \text{integer}[\tau/\Delta]$  and the covariance of the piecewise-constant white noise  $v_{yi}(k)$  is  $\Delta^{-1}[v_{yi}^0(k)/f_i(k)]$  to account for the finite time step. Similarly, the covariance of the motor noise  $v_u(k)$  now becomes  $v_{ui}^0/\Delta$ .

## 2.5 Human Operator Model Equations

Equations (23), (24), and (26) may be combined into an augmented man-model equation, suitable for Monte-Carlo simulation. Defining the augmented state  $x(k) = [x(k), u(k-1)]$ , and input  $w = [w_m, v_u]$ , we obtain

$$\underline{x}(k+1) = \Phi \underline{x}(k) + \Gamma u_c(k) + E w(k) + F z_m(k) \quad (31)$$

$$y(k) = C \underline{x}(k) \quad (32)$$

where  $u_c(k) = L_1 \hat{x}_m(k)$  is the "commanded" control. The augmented matrices are obtained by rewriting Equation (26),

$$u(k) = (I - \Delta L_2)u(k-1) + \Delta u_c(k) + \Delta L_2 v_u(k) \quad (26a)$$

and combining with Equation (23), yielding:

$$\begin{aligned} \Gamma &= \Delta \begin{bmatrix} \Gamma_m \\ I \end{bmatrix} ; \quad F = \Delta \begin{bmatrix} F_m \\ 0 \end{bmatrix} ; \quad E = \Delta \begin{bmatrix} E_m & \Gamma_m L_2 \\ 0 & L_2 \end{bmatrix} \\ \Phi &= \begin{bmatrix} \Phi_m & \Gamma_m (I - \Delta L_2) \\ 0 & (I - \Delta L_2) \end{bmatrix} ; \quad C = \begin{bmatrix} C_m & D_m \end{bmatrix} \end{aligned} \quad (33)$$

The equations (31)-(32) are similar to the discretized equations that occur in the covariance propagation studies using the OCM. Borrowing heavily from earlier efforts, it is easy to write the equations for the Kalman filter-predictor combination that generates the state estimate  $\hat{x}(k)$ . For compatibility with the covariance propagation modeling, we use the a posteriori estimate

$$\hat{x}(k) = \hat{x}(k|k) = E[\underline{x}(k) | y_p(0), \dots, y_p(k)] \quad (34)$$

The Kalman filter generates the (a posteriori) estimate of the delayed state,

$$\hat{p}(k|k) = E[\underline{x}(k-N)|y_p(0), \dots, y_p(k)] \quad (35a)$$

and the (a priori) one-step ahead prediction

$$\hat{p}(k+1|k) = E[\underline{x}(k+1-N)|y_p(0), \dots, y_p(k)] \quad (35b)$$

by means of the usual update and propagate set of equations. These are, respectively:

$$\hat{p}(k|k) = \hat{p}(k|k-1) + G_k v(k) \quad (36a)$$

$$\hat{p}(k+1|k) = \Phi \hat{p}(k|k) + \Gamma u_c(k-N) \quad (36b)$$

where  $v(k)$  is the innovations, or residual sequence

$$v(k) = y_p(k) - C \hat{p}(k|k-1) \quad (37)$$

and the initial condition is

$$\hat{p}(0|-1) = \text{given} = \underline{x}(0) \quad (38)$$

The filter gain  $G_k$  is<sup>(1)</sup>

$$G_k = k|k-1 C' [C k|k-1 C' + \frac{1}{\Delta} v_y(k)]^{-1} \quad (39)$$

where the update-propagate sequence for generating the Riccati solution  $\Sigma$  is:

$$\Sigma_{k|k} = (I - G_k C) \Sigma_{k|k-1} (I - G_k C)' + G_k \frac{\bar{v}_y(k)}{\Delta} G_k' \quad (40a)$$

$$\Sigma_{k|k} = \Phi \Sigma_{k|k} \Phi' + EWE' + FZF' \quad (40b)$$

and

$$W = \text{diag}[w_{mi}(k)/\Delta, v_{ui}(k)/\Delta]$$

$$Z = \text{diag}[\frac{T_{cor}}{\Delta} z_i^2(k)]$$

are "pseudo-noise" covariance matrices. The "correlation time",

$T_{cor} = 1$  sec.

The predictor forms the estimate  $\underline{x}(k)$  from  $\hat{p}(k|k)$  using:

---

(1) For simplicity, the RIDF gain  $N_i$  is included with  $v_y$ , rather than with  $C$ . This is the usual practice in the OCM.

$$\hat{x}(k) = \Phi^N \hat{p}(k|k) + \sum_{i=0}^{N-1} \Phi^i \Gamma u_c(k-i-1) \quad N > 0 \quad (41)$$

If  $N=0$ ,  $\hat{x}(k) = \hat{p}(k|k)$ .

## 2.6 Special Considerations

There are several issues in the simulation of the above equations that remain to be resolved. Some are unique to the man-machine problem.

### 2.6.1 Storage of Delayed Quantities

The simulation equation (41) requires knowledge of the commanded control  $u_c(k-1), \dots, u_c(k-N)$ . The update equation (36b) requires  $u_c(k-N)$ . Similarly, the computation of  $v(k)$  is based on the delayed quantity  $y(k-N)$ . To meet these requirements we retain in storage, at time  $k$ ,

$$PASTUC = [u_c(k-N) \dots u_c(k)] \quad (42a)$$

$$PASTY = [y(k-N) \dots y(k)] \quad (42b)$$

### 2.6.2 On-line Variance Estimation

The diagonal observation noise covariance matrix  $\bar{V}_y$  in Equations (39) and (40a) is given by:

$$\bar{V}_{yi}(k) = \frac{v_y^o(k)}{f_i(k) \hat{N}_i^2(k-N)} \quad i=1, \dots, NYM \quad (43)$$

where  $f_i(k)$  is the fractional attention to  $y_i$  at time  $k$ , and:

$$v_y^o(k) = v_{yi}(k) + \pi \rho_{yi} E[y_i^2(k-N)] \quad (44)$$

$$\hat{N}_i(k-N) = \text{erfc} \left[ \frac{|y_i(k-N)|}{a_i \sqrt{2}} \right]$$

Similarly, the covariance of the motor noise:

$$v_{ui}^o(k) = v_{ui}(k) + \pi \rho_{ui} \text{Var}[u_i(k-1)] \quad i=1, \dots, NUM \quad (45)$$

Both Equations (44) and (45) require process (i.e. ensemble) statistics at time  $k$ . However, these are not available from a single Monte-Carlo trajectory, and their precomputation for subsequent read-in is unfeasible. The approach we have taken is to obtain temporal approximations using filtered past data. An approximation

$$\alpha(k) \doteq E[y_i^2(k-N)]$$

is obtained via 1st-order filtering of  $y_i^2(k-N)$ ,

$$\alpha(k) = e^{-\Delta/\tau_m} \alpha(k-1) + (1 - e^{-\Delta/\tau_m}) y_i^2(k-N) \quad (46)$$

with initial condition  $\alpha(N-1) = y_i^2(0)$ . The approximate variance of  $u_i^2(k-1)$  is found using a two-step procedure that estimates (through filtering) the mean and mean-square, and then computes the variance. The time constant  $\tau_m = 0.5$  sec.

### 2.6.3 Pseudo-Random Noise Sequence

The Monte-Carlo simulation of the human operator equations must generate discrete white-noise sequences for observation noise and motor noise that have specified variances  $\bar{v}_{yi}/\Delta$  and  $v_{ui}^0/\Delta$ , respectively. This accomplished by picking, at time k,

$$v_{ui}(k) = \frac{v_{ui}^0}{\Delta}^{1/2} \xi(k)$$

where  $\xi(k)=N(0,1)$  is a unit variance, zero mean, Gaussian random variable.  $(k)$  is generated by averaging 12 uniformly distributed  $(-1/2, +1/2)$  independent random variables. A slight modification is made when choosing the observation noise sequence, to reflect more precisely the underlying multiplicative noise process. We pick

$$v_{yi}(k) = \frac{\tilde{v}_{yi}}{\Delta}^{1/2} \xi(k)$$

where

$$\tilde{v}_{yi}(k) = \frac{v_{yi} + \pi \rho_i y_i^2(k-N)}{f_i(k) \hat{N}_i^2(k-N)}$$

depends only on the instantaneous value of  $y_i(k-N)$ .

### 2.7 Summary of Human Model Computations

The major part of the man-machine simulation is the implementation of the equations of the OCM, where a control input  $u_k$  is generated from the observations  $y_k$ . The steps in this process are summarized below.

1. Storage of  $y(k)$  in the  $(N+1)$ -st column of PASTY, Eq. (42b).

2. Computation of  $\alpha(k)$  via Eq. (46), and the observation noise covariance  $V_y(k)$  using Eqs. (43)-(44).

3. Computation of the residuals

$$v(k) = y(k-N) + v_y(k) - C\hat{p}(k|k-1) \quad (47)$$

4. Compute the filter gain  $G_k$  via Eq. (3a) and update the Riccati equation (40a) to obtain  $\Sigma_{k|k}$ .

5. Obtain the a posteriori estimate  $\hat{p}(k|k)$ , Eq. (36a).

6. Obtain the state estimate  $\hat{x}(k)$  via Eq. (41).

7. Compute the new commanded control,

$$u_c(k) = -L_1 \hat{x}(k)$$

and store it in the  $(N+1)$ -st column of PASTUC.

8. Generate the piecewise constant control  $u(k)$  to use over the upcoming time interval  $[k, k+1]$  from Eq. (26a).

9. Update the estimate of  $\text{Var}[u(k)]$  for use at the next time step.

10. Propagate  $\Sigma$  and  $\hat{p}$  using Eqs. (40b) and (36b).

11. Do a stack pushdown (i.e., column shift to the left) on PASTY and PASTUC to get ready for the next time step.

### 3. PROGRAM DESCRIPTION

The computer program MCARLO has been developed for simulating the human operator equations, and controlling the parameter updating processes. The program consists of six major routines that are highly modular in structure:

1. MAIN
2. SYSTM
3. UPDATE
4. MAN
5. INFORM
6. PRINTR

along with numerous minor, user supplied routines. The function of each of the above routines is discussed.

#### 3.1 MAIN Program

The MAIN program initializes time and controls the overall program flow according to Figure 1. It calls the required subroutines for system propagation, and information storage. Time is incremented,  $t = t + \Delta$ , and the cycle repeats. When  $t \geq t_f$ , the printout routine is called.

#### 3.2 Subroutine SYSTM

Subroutine SYSTM is a user-oriented routine that simulates the response of the actual system. Given the control input  $u$ , and the external or disturbance inputs  $w$  and  $z$  over the time interval  $(t - \Delta, t]$ , SYSTM returns the value of  $y$  at time  $t$ . At the first time step,  $t = t_0$ , only internal initializations are performed. The present implementation requires SYSTM to compute and return (at time  $t$ ) the values of  $w$  and  $z$  for its own use over the next time interval. As an alternate approach, a separate subroutine EXTINP might perform this function once NW and NZ are known.

The SYSTM subroutine is entirely self-contained. As such it is possible to replace it, in its entirety, by user written routine that simulates the

given system.(2) The only requirement is the generation of  $y(t)$  from control input  $u(t)$  and the disturbance inputs. If the system is time-varying, the logic for updating system parameters must be included within the SYSTEM routine. The system simulation can thus be as complicated or as simple as the problem may warrant.

The SYSTEM subroutine now contained in the MCARLO program treats the general linear case

$$\begin{aligned}\dot{x}(t) &= A_S x(t) + B_S u(t) + E_S w(t) + F_S z(t) \\ x(t^+) &= x(t^-) + \delta x(t) ; \quad x(t_0^-) = 0 \\ y(t) &= C_S x(t) + D_S u(t)\end{aligned}$$

$$\text{cov}[W_i(t)] = W_{Si}^0(t)$$

where any parameter matrix can be time-varying. The method by which parameters are updated is similar to the alphanumeric code/index scheme used in TIVAR. Parameters can be changed at time  $t$  via external or card inputs. They can also be changed periodically via an internal -- user supplied -- subroutine SYSNEW. Table Ia defines the parameter codes for SYSTEM. Note that mnemonics A and not AS, etc., have been used for compatibility with TIVAR deck setups.

At time  $t$  the subroutine updates the pertinent variables and (if necessary) computes new discretize equations. The state is propagated using the transition matrix method. At time  $t_0$  matrices A, B, C must be input for proper initialization. Unless input, D, E, F,  $W_S^0$ ,  $x$  are assumed to be zero. Finally, the parameters associated with codes 1-7 are stored in common blocks. This makes them accessible to other subroutines for the special case when model = system.

---

(2) An analog simulation or a "real" system with A/D interface provides an interesting possibility.

Table Ia: PARAMETER CODES IN SYSTEM

<u>CODE</u>	<u>KEY</u>	<u>DESCRIPTION</u>
A	1	System $A_s$ matrix, NX by NX
B	2	Control $B_s$ matrix, NX by NU
C	3	Output $C_s$ matrix, NY by NX
D	4	Output $D_s$ matrix, NY by NU
E	5	Noise $E_s$ matrix, NX by NW
F	6	Bias input $F_s$ matrix NX by NZ
W0	7	Noise covariances $W_{0s}$ , NW vector
XINC	8	Increment $\delta x$ to system state, NX vector
INT	9	Transfer to subroutine SYSNEW
PRINT	10	Printout interval for data

Table Ib: PARAMETER CODES IN UPDATE

<u>CODE</u>	<u>KEY</u>	<u>DESCRIPTION</u>
AM	1	Model $A_m$ matrix, NXM by NXM
BM	2	Control $B_m$ matrix, NXM by NUM
CM	3	Output $C_m$ matrix, NYM by NXM
DM	4	Output $D_m$ matrix, NYM by NUM
EM	5	Noise $E_m$ matrix, NXM by NWM
FM	6	Bias input $F_m$ matrix, NXM by NZM
WOM	7	Model noise covariances $W_{0m}$ , NWM vector
XHINC	8	Increment $\delta \hat{x}$ to $\hat{p}_{k k-1}$ , NXM vector
TD	9	Human's time delay $\tau$
MNA	10	Additive NUM motor noise variances $V_u$
MNR	11	Motor noise ratios $\rho_u$ , NUM vector
SNA	12	Additive NYM sensor noise variances $V_y$
SNR	13	Sensor noise ratios $\rho_y$ , NYM vector
TH	14	Observational thresholds, $a_i$ , NYM vector
ATTN	15	Attention allocations, $f_i$ , NYM vector
CGAIN	16	Continuous control gains $L_c$ , NUM by NTOT
DGAIN	17	Discrete control gains $L_d$ , NUM by NTOT
INT	18	Transfer to subroutine MANNEW
PRINT	19	Printout interval for data

### 3.3 Subroutine UPDATE

The two major functions of this subroutine are to update the (time-varying) parameters in the human operator model, and to compute the discretized model equations. The parameters are updated using an alphanumeric /code/index scheme. Parameters can be changed at time  $t$  via external or card inputs. They can also be changed periodically via an internal -- user supplied -- subroutine MANNEW. Table Ib defines the codes for UPDATE. The parameters are described in Sections 2.2 - 2.3.

The discretization of the human operator model equations follows the approach in Sections 2.4 - 2.5. A change in either  $A_m$  or  $B_m$  necessitates a recomputation of the discrete system matrices  $\Phi_m$  and/or  $\Gamma_m$ . If continuous time feedback gains  $L_c$  are input, UPDATE computes the equivalent discretized gains  $\hat{L}_d$  using the "average gain" method.

UPDATE initializes all of the man-model parameters to zero,(3) with the exception of  $A_m$ ,  $B_m$ ,  $C_m$ ,  $L_d$  or  $L_c$  which must be input at time  $t_0$ . The subroutine can equate any of the first seven code parameters to their linear system counterparts.

### 3.4 Subroutine MAN

This is the major computational subroutine in the MCARLO program. It performs all of the human model computations summarized in Section 2.7. Thus, the basic function of MAN is to output (at time  $t$ ) the NU control  $u$  to apply to the system over  $(t, t+\Delta]$ . The dynamic inputs to MAN include the NY observations  $y(t)$ , and the value of the deterministic input  $z$  over  $(t, t+\Delta]$ . This latter requirement is expected to be relaxed through future modeling efforts.

### 3.5 Subroutine INFORM

This subroutine is used to store data for subsequent printing and/or plotting. Data is stored on disk files every  $(NPRNT)\Delta$  seconds starting at  $t=t_0$ . For convenience, printed and plotted variables are stored on separate

---

(3) Initial  $f_i = 1$

files. The value of NPRNT is an input parameter to MAIN, but can be changed via either system or update. For the system, any component of  $x$ ,  $y$  or  $u$  may be output as data. For the man-model, any component of  $\hat{x}$ ,  $\hat{y}$  or  $v$  may be output where  $\hat{y} = C\hat{x}$ .

### 3.6 Subroutine PRINTR

This routine, called the first time  $t \geq t_F$ , outputs the stored time histories of the selected variables. For plotted variables, an automatic scaling feature is used.

### 3.7 Program Operation

MCARLO has been designed to generate Monte-Carlo time histories of the signals in a man-machine control task. Each run of MCARLO generates one sample path. To obtain more elements in the ensemble it is necessary to make additional computer runs, using different values for the random number generator seed. The sample waveforms can all be stored for later ensemble averaging. As the number of samples  $N_s \rightarrow \infty$ , the sample statistics should converge to the ensemble (covariance) statistics that are computed by TIVAR.

#### 4. INPUT DECK SETUP

There are three sections of input data for MCARLO as discussed below. In addition, there are three user-written subroutines: SYSNEW, MANNEW, and FDET.

##### 4.1 Control Cards

There are 5 major control cards that are required by the MAIN program.

###### Card 1 - Title Information

Column 1: blank

Columns 2-80: alphanumeric title information

###### Card 2 - Random Number Seed, I10 Format

Field 1: IXYZ = any integer

###### Card 3 - Time Information, 3E10.0, I10 Format

Field 1: DEL = discrete time step (sec)

Field 2: T0 = initial time (sec)

Field 3: TF = final time (sec)

Field 4: NPRNT = printout frequency (integer)

###### Card 4 - Print/Plot Information for System Variables, 3(20I1) Format

Field 1: Print/Plot codes for states 1 - NX

Field 2: Print/Plot codes for outputs 1 - NY

Field 3: Print/Plot codes for controls 1 - NU

###### Card 5 - Print/Plot Information for Model Variables, 3(20I1) Format

Field 1: Print/Plot codes for state estimates 1 - NXM

Field 2: Print/Plot codes for output estimates 1 - NYM

Field 3: Print/Plot codes for KF residuals 1 - NYM

Note that on cards 4-5 each column of an associated field corresponds to one state, output estimate, etc. A single integer governs the printing or plotting of the time history of the variable:

0, or blank = no printing or plotting of the variable  
1 = print time history vs. time  
3 = plot time history vs. time  
2 = print and plot time history vs. time

A maximum of 10 of any variables (e.g. states or outputs) can be printed on wide paper.

#### 4.2 System Parameter Cards

These cards are used to change system parameters in the linear case. If the user supplies his own SYSTM subroutine, this section of data is omitted, or replaced by problem specific data cards.

##### Card 1 - Frequencies for internal time breaks, NDTS, 10I5 Format

The 10 fields are associated with the 10 system parameter cards (see Table IIa) on a one-to-one basis. The I-th field is associated with Code I. NDTS(I) is the frequency (number of time steps) at which subroutine SYSNEW is to be called internally with KEY=I, starting at time T0. Calling SYSNEW with KEY=I sets ISFLAG(I)=1 for one time step. The actual parameter values must be changed internally by user-written code. If no code is supplied, the associated parameters retain their value.

Remaining Cards - These are used to change system parameters via external read-in at specified times. The deck setup follows a standard form.

##### Time Card - Cols. 1-4 Alphanumeric TIME

Cols. 11-20 Time of external break E10.0

##### Code Card - Cols. 1-5 One of the Alphanumeric codes in Table IIa

Cols. 8-10 Index NQQ for dimension information, I3

##### Parameter Cards - The new parameter values required by the code.

Table IIa: SYSTEM PARAMETER CARD INPUTS

<u>CODE</u>	<u>KEY</u>	<u>INDEX</u>	<u>INPUT DATA</u>	<u>INITIAL VALUE</u>
A	1	NX	$(A_s)_{ij} \quad i=1, \dots, NX, \quad j=1, \dots, NX$	undef
B	2	NU	$(B_s)_{ij} \quad i=1, \dots, NX, \quad j=1, \dots, NU$	undef
C	3	NY	$(C_s)_{ij} \quad i=1, \dots, NY, \quad j=1, \dots, NX$	undef
D	4	NY	$(C_s)_{ij} \quad i=1, \dots, NY, \quad j=1, \dots, NU$	0
E	5	NW	$(E_s)_{ij} \quad i=1, \dots, NX, \quad j=1, \dots, NW$	0
F	6	NZ	$(F_s)_{ij} \quad i=1, \dots, NX, \quad j=1, \dots, NZ$	0
WO	7	NW	$(W_o)_i \quad i=1, \dots, NW$	0
XINC	8	---	$(\delta_x)_i \quad i=1, \dots, NW$	0
INT	9	KEY	---	---
PRINT	10	NPRNT	---	---

Table IIb: MAN-MODEL PARAMETER CARD INPUTS

<u>CODE</u>	<u>KEY</u>	<u>INDEX</u>	<u>INPUT DATA</u>	<u>INITIAL VALUE</u>
AM	1	NXM*	$(A_m)_{ij} \quad i=1, \dots, NXM, \quad j=1, \dots, NXM$	undef
BM	2	NUM*	$(B_m)_{ij} \quad i=1, \dots, NXM, \quad j=1, \dots, NUM$	undef
CM	3	NYM*	$(C_m)_{ij} \quad i=1, \dots, NYM, \quad j=1, \dots, NXM$	undef
DM	4	NYM*	$(D_m)_{ij} \quad i=1, \dots, NYM, \quad j=1, \dots, NUM$	0
EM	5	NWM*	$(E_m)_{ij} \quad i=1, \dots, NXM, \quad j=1, \dots, NWM$	0
FM	6	NZM*	$(F_m)_{ij} \quad i=1, \dots, NZM, \quad j=1, \dots, NZM$	0
WOM	7	NWM*	$(W_m^o)_i \quad i=1, \dots, NWM$	0
XHINC	8	---	$(\delta_p)_i \quad i=1, \dots, NXM$	0
TD	9	---	$\tau$	0
MNA	10	---	$V_{ui} \quad i=1, \dots, NUM$	0
MNR	11	---	$\rho_{ui} \quad i=1, \dots, NUM$ in dB	- dB
SNA	12	---	$V_{yi} \quad i=1, \dots, NYM$	0
SNR	13	---	$\rho_{yi} \quad i=1, \dots, NYM$	- dB
TH	14	---	$a_i \quad i=1, \dots, NYM$	0
ATTN	15	---	$f_i \quad i=1, \dots, NYM$	1
CGAIN	16	---	$(L_c)_{ij} \quad i=1, \dots, NUM, \quad j=1, \dots, NXM+NUM$	undef
DGAIN	17	---	$(L_d)_{ij} \quad i=1, \dots, NUM < j=1, \dots, NXM+NUM$	undef
INT	18	KEY	---	---
PRINT	19	NPRNT	---	---

\*If <0, model parameters are automatically equated to system parameters, and no input data is needed.

The sequence of code card followed by new parameter values is repeated for all items that the user wishes to change at the given time. To change parameters at the next time, input a new time card, followed by a code card, input the parameter values, code card, etc. When using external (card) updates, the following rules must be observed:

1.  $NX + NU \leq 15$
2. Time breaks must occur in increasing order.
3. Parameter cards should occur in the sequence listed in Table IIa. Thus, codes with lower KEY numbers should be read in first.
4. The parameter cards must be input immediately following the associated code card.
5. The last system parameter card must be an end-system card, containing the alphanumeric ENDS in cols. 1-4.
6. If they occur at the same time, external updates take precedence over internal updates.

The program reads all of the system update cards at the first time step, and stores all the information on a disk file for sequential read-in.

#### 4.3 Man-Model Parameter Cards

These cards are used to change man-model parameters either internally in periodic mode, or via external card inputs. The deck setup is virtually identical in form to the previous section.

##### Cards 1-2 - Frequencies for internal time breaks, NDTM, 19I5 Format

The 19 fields, spread over 2 cards, are associated with the 19 man-model parameter codes (see Table IIb) on a one-to-one basis. NDTM(I) is the frequency (number of time steps) at which the user supplied subroutine MANNEW is to be called internally with KEY=I. The operation is similar to that for SYSNEW.

Remaining Cards - These are used to change man-model parameters via external read-in at specified times. The deck setup follows the standard form as in the previous section 4.2:

Time Card - Cols. 1-4 Alphanumeric TIME

                  Cols. 11-20 Time of external break E10.0

Code Card - Cols. 1-5 One of the Alphanumeric codes in Table IIb

                  Cols. 8-10 Index NQQ for dimension information

Parameter Cards - As required by the associated code.

The sequence of code card - parameter card is repeated for all items the user wishes to change at the given time. To change parameters at the next time, the above three part sequence is repeated. The following rules must be observed:

1.  $NXM + NUM \leq 15$   
    NUM = NU  
    NYM = NY  
    NZM = NZ (or NZM = 0)
2. Time breaks must occur in increasing order.
3. Parameter codes should occur in the sequence listed in Table IIb. Thus, codes should be sorted for reading according to increasing KEY numbers.
4. The parameter cards must be input immediately following the associated code card, unless  $NQQ \leq 0$  for codes 1-7.
5. The last man-model parameter card must be an end-man card, containing the alphanumeric ENDM in cols. 1-4.
6. If they occur at the same time, external updates take precedence over internal updates.

A useful option is included for any of codes 1-7. If the specified  $NQQ \leq 0$ , man-model parameters are automatically set equal to the corresponding system parameters in the linear case. Also, no read-in of model parameters is done.

#### 4.4 Entering Parameter Data

Data is entered on the parameter cards in 8E10.0 Format, i.e., in floating point fields of 10 columns with a maximum of 8 fields per card. The numbers may be either in fixed-point (decimal) form or in scientific (exponential) form with the exponent right justified in the field. Matrices are entered one row at a time. If a row contains more than 8 entries, continue on a second card for that row. A new row always begins on a new card. Vectors are entered in similar 8E10.0 format: the first entry in the first field, second entry in the second field, etc.

#### 4.5 User Written Routines

The three user written routines are SYSNEW(KEY), MANNEW (KEY), and FDET(K,T). The purpose of the first two routines for changing system and man-model parameters has been discussed earlier. The function FDET(K,T) is used to generate the time history of the deterministic (bias) inputs  $z_i(t)$ . Thus, at time T, and for inputs K,  $K=1, \dots, NZ$ ,

$$FDET(K, T) = Z_K(T)$$

The user must supply his own code for FDET.

## 5. SAMPLE PROBLEM

A sample problem illustrating many of the features of the MCARLO program is given in this section. A description of the problem is presented first, followed by a listing of the user written subroutines, the input data deck, and a listing of the output.

### 5.1 Sample Problem Description

This problem analyzes an AAA tracking task. The controller tracks the azimuth angle of a target which is executing a level fly-by. The key element illustrated by this problem is the use of the FDET function to generate the time history of the deterministic input, i.e. the azimuth trajectory of the target.

The controller is explicitly presented with a display of the azimuth sighting error, and is assumed to derive the corresponding error rate. His task is to minimize this error by controlling a set of rate-aided second-order sight dynamics, his control being a hand-crank.

The target being tracked is executing a constant speed straight and level fly-by of 44 sec duration. The range of the target at crossover,  $R_c$ , is 3000 ft, and the speed, V, is 733 ft/sec producing a maximum azimuth angular velocity of about 14 deg/sec at crossover. Initially, 22 sec before crossover, the target is 16,126 ft from the crossover point, its azimuth angular position is -79.46 deg, and its azimuth angular velocity is 0.4683 deg/sec.

The system states are defined as follows:

- $x_1$  = target azimuth angular position (degrees)
- $x_2$  = target azimuth angular velocity (deg/sec)
- $x_3$  = sight azimuth angular position (degrees)
- $x_4$  = sight azimuth angular velocity (deg/sec)
- $x_5$  = integral of the control input

It is assumed that the controller employs a "constant velocity" model of the target position. Consequently, the state space equations for the first two states (the deterministic states) are:

$$\dot{x}_1(t) = x_2(t)$$

$$\dot{x}_2(t) = z(t),$$

where  $z(t)$ , the deterministic input is the azimuth angular acceleration of the target. Thus,  $z(t)$  is given by:

$$z(t) = -2(V/R_c)^2 \frac{D(t)/R_c}{(1 + (D(t)/R_c)^2)^2} \quad (47)$$

where

$V$  = the speed of the target = 733 ft/sec

$R_c$  = the range of the target at crossover = 3000 ft

$D(t)$  = the distance of the target from the crossover point

$$= D_0 + Vt = -16,126 + 733t$$

The FDET function computes  $z(t)$  according to Eq. 47.

The transfer function relating the sight position to the control input is:

$$\frac{x_3(s)}{u(s)} = \frac{64(s+1)}{s(s^2+12s+64)} = (1+1/s) \frac{64}{s^2+12s+64} \quad (48)$$

Consequently, the state space equations for the last three states (the controllable states) are:

$$\dot{x}_3 = x_4$$

$$\dot{x}_4 = -64x_3(t) - 12x_4(t) + 64x_5(t) + 64u(t) \quad (49)$$

$$\dot{x}_5 = u(t)$$

The displayed outputs are the azimuth sighting error and error rate and are given by:

$$y_1(t) = x_1(t) - x_3(t) \quad (50)$$

$$y_2(t) = x_2(t) - x_4(t)$$

Regarding the human's inherent limitations, the observation noise to signal ratio (SNR) and motor noise ratio (MNR) are set to the nominal values of -20dB and -25dB, respectively. The perceptual time delay (TD) is set to 0.20 sec. Observational thresholds are set at 0.05 deg for  $y_1$  (corresponding to 1% of the field of view of the gunsight), and 0.025 deg for  $y_2$  (corresponding to a nominal differential threshold for motion).

The control gains, CGAIN, computed by another program, were chosen by setting the cost on error to unity, and adjusting the cost on control rate to produce a neuro-motor lag  $T_N$  of 0.1 sec.

Finally, since the mean initial states are far from zero, the human's estimator requires some time to settle down. The presence of the human's time delay further compounds this problem. To provide an initializing transition period while the human's estimator settles down, the sample problem is started at  $t=-6.0$  sec, at which time the target is 20,524 ft from the crossover point, its azimuth angular position is -81.684 deg and its azimuth angular velocity is 0.2928 deg/sec. During this initialization period, the human's time delay is set to zero, and printouts are suppressed. At  $t=0$ , however, the time delay is set to 0.20 sec, and the printout interval is set to 1 sec.

The states are incremented, XINC, so that the initial angular position and velocity of the target are correct, and the human's state estimates are incremented, XHINC, so that the initial error and error rate are zero.

5.2 User Written Subroutines for the Sample Problem

```
C      MCP - PROBLEM DEPENDENT SUBPROGRAMS FOR MCARLO
C      INCLUDES:
C          1 - FUNCTION FDET
C          2 - SUBROUTINE SYSNEW
C          3 - SUBROUTINE MANNEW

C      FUNCTION FDET(NQT,T)
C      GENERATES DETERMINISTIC INPUT

C      DATA
1      X0, Y0, V0 /-16126.0, 3000.0, 733.0/,
2      R /57.296/

X=X0+V0*T
A=X/Y0
B=1.0+A*A
C=(V0/Y0)/B
D=-2.0*A*C*C
FDET=R*D
RETURN

END

C      SUBROUTINE SYSNEW(NQQ)
C      INTERNAL UPDATES TO THE SYSTEM

RETURN
END

C      SUBROUTINE MANNEW(NQQ)
C      INTERNAL UPDATES TO THE MAN

RETURN
END
```

5.3 Input deck for the Sample Problem

P-I-D CONTROLLER. MONTE-CARLO SIMULATION

56315	0.05	-6.0	44.0	120								
22221		22			2							
10100	0	0	0	0	0	0	0	0	0	0	0	0
A	5											
	0.0		1.0		0.0		0.0		0.0			
	0.0		0.0		0.0		0.0		0.0			
	0.0		0.0		0.0		1.0		0.0			
	0.0		0.0		-64.0		-12.0		64.0			
	0.0		0.0		0.0		0.0		0.0			
B	1											
	0.0											
	0.0											
	0.0											
	64.0											
	1.0											
F	1											
	0.0											
	1.0											
	0.0											
	0.0											
C	2											
	1.0		0.0		-1.0		0.0		0.0			
	0.0		1.0		0.0		-1.0		0.0			
D	2											
	0.0											
	8.0											
XINC												
	-81.684		0.2928		-81.684		0.2928		0.0			
ENDS												
	0	0	0	0	0	0	0	0	0	0	0	0
	0	0	0	0	0	0	0	0	0	0	0	0
AM	0											
BM	0											
CM	0											
DM	0											
FM	0											
XHINC												
	-81.684		0.2928		-81.684		0.2928		0.0			
TD	0.00											
CGAIN												
	-15.39		-3.303		6.359		0.6404		9.034			
	10.00											
MNR	-25.0											
SNR	-20.0		-20.0									
TH	0.05		0.025									
TIME	0		0.0									
TD	0.20											
PRINT	20											
ENDM												

5.4 Output listing for the Sample Problem

STARTING MCARLO  
2-Dec-76 14:20

P-I-D CONTROLLER. MONTE-CARLO SIMULATION

RANDOM NUMBER SEED= 56315  
 INTEGRATION TIME STEP = 0.050  
 INITIAL TIME = -6.000  
 TERMINAL TIME = 44.000  
 PRINTOUT FREQUENCY = 120  
 SYSTEM INTERNAL BREAKS INDEX CODE NDT

SYSTEM EXTERNAL BREAK AT T=	-6.000	CODE A	INDEX= 5
0.000E-01	1.000E+00	0.000E-01	0.000E-01
0.000E-01	0.000E-01	0.000E-01	0.000E-01
0.000E-01	0.000E-01	0.000E-01	1.000E+00
0.000E-01	0.000E-01	-6.400E+01	-1.200E+01
0.000E-01	0.000E-01	0.000E-01	0.000E-01

SYSTEM EXTERNAL BREAK AT T= -6.000 CODE B INDEX= 1

0.000E-01	0.000E-01	0.000E-01	6.400E+01
1.000E+00			

SYSTEM EXTERNAL BREAK AT T= -6.000 CODE F INDEX= 1

0.000E-01	1.000E+00	0.000E-01	0.000E-01
0.000E-01	0.000E-01	0.000E-01	0.000E-01

SYSTEM EXTERNAL BREAK AT T= -6.000 CODE C INDEX= 2

1.000E+00	0.000E-01	-1.000E+00	0.000E-01
0.000E-01	1.000E+00	0.000E-01	-1.000E+00

SYSTEM EXTERNAL BREAK AT T= -6.000 CODE D INDEX= 2

0.000E-01	0.000E-01		
-----------	-----------	--	--

SYSTEM EXTERNAL BREAK AT T= -6.000 CODE XINC INDEX= 0

-8.168E+01	2.928E-01	-8.168E+01	2.928E-01
------------	-----------	------------	-----------

HUMAN INTERNAL BREAKS INDEX CODE NDT

			0.000E-01
--	--	--	-----------

HUMAN EXTERNAL BREAK AT T= -6.000 CODE AM INDEX= 0

HUMAN MODEL = SYSTEM

HUMAN EXTERNAL BREAK AT T= -6.000 CODE BM INDEX= 0

HUMAN MODEL = SYSTEM

HUMAN EXTERNAL BREAK AT T= -6.000 CODE CM INDEX= 0

HUMAN MODEL = SYSTEM

HUMAN EXTERNAL BREAK AT T= -6.000 CODE DM INDEX= 0

HUMAN MODEL = SYSTEM

HUMAN EXTERNAL BREAK AT T= -6.000 CODE FM INDEX= 0

HUMAN MODEL = SYSTEM

HUMAN EXTERNAL BREAK AT T= -6.000 CODE XHINC INDEX= 0

-8.168E+01	2.928E-01	-8.168E+01	2.928E-01
------------	-----------	------------	-----------

HUMAN EXTERNAL BREAK AT T=	-6.000	CODE	TD	INDEX=	0
0.000E-01					
HUMAN EXTERNAL BREAK AT T=	-6.000	CODE	CGAIN	INDEX=	0
-1.539E+01	-3.303E+00	6.359E+00	6.404E-01	9.034E+00	
1.000E+01					
HUMAN EXTERNAL BREAK AT T=	-6.000	CODE	MNR	INDEX=	0
-2.500E+01					
HUMAN EXTERNAL BREAK AT T=	-6.000	CODE	SNR	INDEX=	0
-2.000E+01	-2.000E+01				
HUMAN EXTERNAL BREAK AT T=	-6.000	CODE	TH	INDEX=	0
5.000E-02	2.500E-02				
EQUIVALENT DISCRETE GAINS GENERATED:					
-1.187E+01	-2.871E+00	4.078E+00	4.587E-01	7.791E+00	
8.741E+00					
HUMAN EXTERNAL BREAK AT T=	0.000	CODE	TD	INDEX=	0
2.000E-01					
HUMAN EXTERNAL BREAK AT T=	0.000	CODE	PRINT	INDEX=	20
MEAN OF X VECTOR					
-9.974E+00	3.223E+00	-9.863E+00	3.199E+00	-1.080E+01	
RMS VALUES OF X VECTOR					
6.586E+01	3.843E+00	6.585E+01	1.257E+01	6.407E+01	
MEAN OF Y VECTOR					
-1.112E-01	2.335E-02				
RMS VALUES OF Y VECTOR					
2.074E+00	1.195E+01				
MEAN OF U VECTOR					
1.580E+00					
RMS VALUES OF U VECTOR					
9.259E+00					

TIME	STATE 1	STATE 2	STATE 3	STATE 4	STATE 5
0.00	-7.947E+01	4.677E-01	-7.960E+01	4.125E-01	-7.974E+01
1.00	-7.898E+01	5.116E-01	-7.915E+01	9.271E-01	-7.943E+01
2.00	-7.844E+01	5.618E-01	-7.845E+01	5.847E-01	-7.888E+01
3.00	-7.786E+01	6.197E-01	-7.789E+01	7.591E-01	-7.833E+01
4.00	-7.721E+01	6.868E-01	-7.726E+01	7.768E-01	-7.773E+01
5.00	-7.648E+01	7.653E-01	-7.651E+01	8.245E-01	-7.707E+01
6.00	-7.567E+01	8.577E-01	-7.565E+01	8.815E-01	-7.629E+01
7.00	-7.477E+01	9.675E-01	-7.480E+01	7.255E-01	-7.546E+01
8.00	-7.374E+01	1.099E+00	-7.383E+01	1.253E+00	-7.458E+01
9.00	-7.257E+01	1.258E+00	-7.258E+01	1.210E+00	-7.349E+01
10.00	-7.122E+01	1.454E+00	-7.121E+01	1.464E+00	-7.227E+01
11.00	-6.965E+01	1.696E+00	-6.964E+01	1.852E+00	-7.086E+01
12.00	-6.782E+01	2.000E+00	-6.780E+01	1.842E+00	-6.921E+01
13.00	-6.564E+01	2.388E+00	-6.563E+01	2.699E+00	-6.729E+01
14.00	-6.303E+01	2.890E+00	-6.297E+01	2.853E+00	-6.499E+01
15.00	-5.984E+01	3.548E+00	-6.001E+01	4.086E+00	-6.228E+01
16.00	-5.590E+01	4.421E+00	-5.591E+01	4.590E+00	-5.887E+01
17.00	-5.095E+01	5.584E+00	-5.114E+01	5.437E+00	-5.472E+01
18.00	-4.467E+01	7.117E+00	-4.506E+01	7.672E+00	-4.956E+01
19.00	-3.667E+01	9.054E+00	-3.690E+01	8.665E+00	-4.282E+01
20.00	-2.658E+01	1.125E+01	-2.679E+01	1.159E+01	-3.428E+01
21.00	-1.436E+01	1.317E+01	-1.511E+01	1.323E+01	-2.380E+01
22.00	-6.721E-01	1.400E+01	-1.157E+00	1.569E+01	-1.150E+01
23.00	1.310E+01	1.325E+01	1.343E+01	1.394E+01	2.197E+00
24.00	2.550E+01	1.136E+01	2.582E+01	1.036E+01	1.535E+01
25.00	3.581E+01	9.160E+00	3.607E+01	8.595E+00	2.708E+01
26.00	4.401E+01	7.204E+00	4.423E+01	6.746E+00	3.684E+01
27.00	5.045E+01	5.651E+00	5.116E+01	4.902E+00	4.485E+01
28.00	5.551E+01	4.471E+00	5.603E+01	4.033E+00	5.108E+01
29.00	5.954E+01	3.586E+00	5.972E+01	3.544E+00	5.599E+01
30.00	6.279E+01	2.919E+00	6.311E+01	3.580E+00	6.001E+01
31.00	6.546E+01	2.410E+00	6.549E+01	2.432E+00	6.314E+01
32.00	6.767E+01	2.018E+00	6.781E+01	1.735E+00	6.580E+01
33.00	6.954E+01	1.710E+00	6.959E+01	1.648E+00	6.796E+01
34.00	7.113E+01	1.465E+00	7.121E+01	1.437E+00	6.979E+01
35.00	7.250E+01	1.267E+00	7.265E+01	1.688E+00	7.136E+01
36.00	7.368E+01	1.106E+00	7.374E+01	1.194E+00	7.270E+01
37.00	7.472E+01	9.735E-01	7.479E+01	8.909E-01	7.388E+01
38.00	7.564E+01	8.627E-01	7.569E+01	8.773E-01	7.489E+01
39.00	7.646E+01	7.696E-01	7.647E+01	7.686E-01	7.579E+01
40.00	7.719E+01	6.905E-01	7.721E+01	6.342E-01	7.659E+01
41.00	7.785E+01	6.228E-01	7.787E+01	5.325E-01	7.731E+01
42.00	7.844E+01	5.645E-01	7.841E+01	5.063E-01	7.793E+01
43.00	7.898E+01	5.139E-01	7.896E+01	4.871E-01	7.850E+01

TIME	OUTPUT 1	OUTPUT 2
0.00	1.374E-01	5.519E-02
1.00	1.656E-01	-4.155E-01
2.00	2.328E-03	-2.293E-02
3.00	3.037E-02	-1.395E-01
4.00	5.052E-02	-9.001E-02
5.00	2.552E-02	-5.922E-02
6.00	-2.732E-02	-2.384E-02
7.00	3.871E-02	2.420E-01
8.00	0.750E-02	-1.538E-01
9.00	1.187E-02	4.863E-02
10.00	-3.470E-03	-9.822E-03
11.00	-1.513E-02	-1.561E-01
12.00	-1.551E-02	1.587E-01
13.00	-1.112E-02	-3.106E-01
14.00	-5.234E-02	3.662E-02
15.00	1.711E-01	-5.383E-01
16.00	1.513E-02	-1.693E-01
17.00	1.836E-01	1.468E-01
18.00	3.834E-01	-5.552E-01
19.00	2.285E-01	3.886E-01
20.00	2.084E-01	-3.483E-01
21.00	7.453E-01	-5.167E-02
22.00	4.852E-01	-1.686E+00
23.00	-3.329E-01	-6.948E-01
24.00	-3.137E-01	9.963E-01
25.00	-2.618E-01	5.649E-01
26.00	-2.212E-01	4.583E-01
27.00	-7.117E-01	7.491E-01
28.00	-5.173E-01	4.380E-01
29.00	-1.845E-01	4.247E-02
30.00	-3.179E-01	-6.614E-01
31.00	-3.509E-02	-2.130E-02
32.00	-1.338E-01	2.827E-01
33.00	-5.400E-02	6.138E-02
34.00	-7.917E-02	2.728E-02
35.00	-1.501E-01	-4.204E-01
36.00	-5.901E-02	-8.793E-02
37.00	-7.014E-02	8.256E-02
38.00	-4.147E-02	-1.456E-02
39.00	-1.335E-02	9.882E-04
40.00	-1.330E-02	5.629E-02
41.00	-1.702E-02	9.026E-02
42.00	3.559E-02	5.817E-02
43.00	2.873E-02	2.686E-02

TIME	CONTROL 1
0.00	1.485E-01
1.00	4.880E-01
2.00	5.266E-01
3.00	6.098E-01
4.00	6.487E-01
5.00	7.193E-01
6.00	8.189E-01
7.00	8.221E-01
8.00	1.016E+00
9.00	1.137E+00
10.00	1.303E+00
11.00	1.553E+00
12.00	1.752E+00
13.00	2.160E+00
14.00	2.563E+00
15.00	3.119E+00
16.00	3.814E+00
17.00	4.742E+00
18.00	5.922E+00
19.00	7.472E+00
20.00	9.740E+00
21.00	1.151E+01
22.00	1.352E+01
23.00	1.364E+01
24.00	1.246E+01
25.00	1.050E+01
26.00	8.561E+00
27.00	6.933E+00
28.00	5.321E+00
29.00	4.479E+00
30.00	3.609E+00
31.00	2.831E+00
32.00	2.292E+00
33.00	1.939E+00
34.00	1.693E+00
35.00	1.536E+00
36.00	1.241E+00
37.00	1.073E+00
38.00	9.634E-01
39.00	8.557E-01
40.00	7.458E-01
41.00	6.433E-01
42.00	5.878E-01
43.00	5.449E-01

TIME	XMHAT 1	XMHAT 3
0.00	-7.975E+01	-7.980E+01
1.00	-7.911E+01	-7.924E+01
2.00	-7.847E+01	-7.848E+01
3.00	-7.782E+01	-7.786E+01
4.00	-7.718E+01	-7.723E+01
5.00	-7.646E+01	-7.648E+01
6.00	-7.559E+01	-7.561E+01
7.00	-7.478E+01	-7.477E+01
8.00	-7.372E+01	-7.380E+01
9.00	-7.256E+01	-7.257E+01
10.00	-7.122E+01	-7.120E+01
11.00	-6.962E+01	-6.965E+01
12.00	-6.784E+01	-6.782E+01
13.00	-6.560E+01	-6.568E+01
14.00	-6.290E+01	-6.296E+01
15.00	-5.981E+01	-5.998E+01
16.00	-5.584E+01	-5.590E+01
17.00	-5.095E+01	-5.109E+01
18.00	-4.481E+01	-4.512E+01
19.00	-3.670E+01	-3.685E+01
20.00	-2.652E+01	-2.672E+01
21.00	-1.464E+01	-1.523E+01
22.00	-6.236E-01	-1.045E+00
23.00	1.317E+01	1.346E+01
24.00	2.546E+01	2.585E+01
25.00	3.575E+01	3.610E+01
26.00	4.408E+01	4.419E+01
27.00	5.020E+01	5.110E+01
28.00	5.542E+01	5.599E+01
29.00	5.973E+01	5.994E+01
30.00	6.308E+01	6.326E+01
31.00	6.570E+01	6.571E+01
32.00	6.786E+01	6.801E+01
33.00	6.973E+01	6.974E+01
34.00	7.130E+01	7.137E+01
35.00	7.276E+01	7.279E+01
36.00	7.385E+01	7.387E+01
37.00	7.487E+01	7.491E+01
38.00	7.582E+01	7.579E+01
39.00	7.660E+01	7.657E+01
40.00	7.731E+01	7.731E+01
41.00	7.794E+01	7.797E+01
42.00	7.853E+01	7.852E+01
43.00	7.906E+01	7.906E+01

TIME	YMHAT 1
0.00	5.440E-02
1.00	1.286E-01
2.00	6.689E-03
3.00	3.072E-02
4.00	4.954E-02
5.00	1.996E-02
6.00	1.385E-02
7.00	-4.005E-03
8.00	7.715E-02
9.00	1.180E-02
10.00	-2.016E-02
11.00	2.993E-02
12.00	-2.005E-02
13.00	7.405E-02
14.00	6.200E-02
15.00	1.700E-01
16.00	5.668E-02
17.00	1.398E-01
18.00	3.162E-01
19.00	1.494E-01
20.00	2.030E-01
21.00	5.901E-01
22.00	4.217E-01
23.00	-2.861E-01
24.00	-3.876E-01
25.00	-3.435E-01
26.00	-1.058E-01
27.00	-9.002E-01
28.00	-5.654E-01
29.00	-2.010E-01
30.00	-1.746E-01
31.00	-1.552E-02
32.00	-1.482E-01
33.00	-3.513E-03
34.00	-6.806E-02
35.00	-2.637E-02
36.00	-2.666E-02
37.00	-3.475E-02
38.00	3.157E-02
39.00	2.213E-02
40.00	1.101E-03
41.00	-2.961E-02
42.00	1.100E-02
43.00	1.246E-03

TIME	INOVAT 1
0.00	4.335E+03
1.00	8.887E-02
2.00	-2.526E+02
3.00	-6.851E-02
4.00	-2.569E-01
5.00	1.350E-01
6.00	2.387E-02
7.00	-7.828E-01
8.00	2.523E-01
9.00	1.157E+03
10.00	-9.278E+00
11.00	3.482E-01
12.00	2.497E-02
13.00	-2.527E-01
14.00	8.503E+02
15.00	-1.960E-01
16.00	2.483E-01
17.00	-3.536E-02
18.00	3.922E-01
19.00	1.561E-01
20.00	-1.411E-01
21.00	6.618E-01
22.00	2.696E-01
23.00	-5.703E-02
24.00	-7.549E-01
25.00	-4.178E-01
26.00	2.654E-01
27.00	-1.585E-01
28.00	2.572E-01
29.00	-1.941E-01
30.00	-1.921E-01
31.00	7.584E-02
32.00	-3.820E-02
33.00	-9.707E-02
34.00	-1.796E-01
35.00	1.117E-01
36.00	-2.200E-01
37.00	-5.386E-02
38.00	-5.220E-02
39.00	1.576E-01
40.00	3.340E-01
41.00	-9.230E-02
42.00	1.300E-01
43.00	-1.188E+00

STATE 1

STATE 2

STATE 3

STATE 4

**OUTPUT**

The figure displays a 2D grid of data points. The horizontal axis (x-axis) is labeled with values  $-1.686\text{E}+00$ ,  $0.00\text{E}-01$ , and  $1.686\text{E}+00$ . The vertical axis (y-axis) is also labeled with values  $-1.686\text{E}+00$ ,  $0.00\text{E}-01$ , and  $1.686\text{E}+00$ . The data points are represented by '+' and 'X' symbols. A central vertical column of '+' symbols is flanked by two diagonal bands of 'X' symbols, creating a cross-like pattern. The '+' symbols are also arranged in a diamond-like shape around the center.

OUTPUT 2

X 0.00E-01 X 1.364E+01

1.485E-01 X

X 4.30E+01

CONTROL 1

X 0.00E-01 X 5.901E-01

X 4.30E+01 X -9.002E-01

YMHA T 1

The figure is a scatter plot with two data series. The x-axis is labeled at -2.526E+02 and 4.335E+03, with intermediate tick marks every 10 units. The y-axis is labeled at 0.00E-01 and 1.00E+01, with intermediate tick marks every 1 unit. The first data series consists of 'X' symbols, forming a vertical column near the left edge of the plot. The second data series consists of '+' symbols, forming a vertical column near the right edge. There are also two isolated 'X' symbols located in the upper-middle section of the plot area.

INOVAT 1  
STOPPING MCARLO

## 6. COMMON BLOCK USAGE

Named COMMON blocks are used to store most data arrays and to pass information among the various subroutines. These are described below.

## 1. /PLOT1/

Required inputs for lineprint plot subroutine

## 2. /INOU/ KIN, KOUT, KPTR, KPUNCH, KDISK, IPOS, IGOS

Logical unit numbers for I-O devices and disks for storage of system parameters and generated data.

## 3. /INFO/

Storage of print/plot information including number of variables, min and max values for plot scaling, etc.

## 4. /TIMES/ TIME, DEL, TO, TF, NPRNT

Time information  $t$ ,  $\Delta$ ,  $t_o$ ,  $t_f$ , printout frequency

## 5. /MAIN1/ NDIM, NDIM1, COM1 /MAIN2/ COM2

Common blocks required for library subroutines

## 6. /SYSX/ NX, NU, BS, AS

Linear System state parameters  $BS=B_S$ ,  $AS=A_S$

## 7. /SYSAD/ BD, AD

Discrete System parameters  $BD=\Gamma_S$ ,  $AD=\Phi_S$

## 8. /SYSY/ NY, DS, CS

Linear System output parameters  $DS=D_S$ ,  $CS=C_S$

## 9. /SYSW/ NW, W0, ES /SYSZ/ NZ, FS

External System input parameters  $W0=W_0$ ,  $ES=E_S$ ,  $FS=F_S$

## 10. /SYSINC/ XINC

State increment  $\delta x$

## 11. /MANX/ NXM, NUM, BM, AM

Man-model state parameters  $BM=B_m$ ,  $AM=A_m$

12. /MANAD/ BD, AD

Augmented discretized Man-model parameters  $BD=\Gamma$ ,  $AD=\Phi$

13. /MANY/ NYM, DM, CM

Man-model output parameters  $DM=D_m$ ,  $CM=C_m$  (augmented)

14. /MANW/ NWM, WOM, EM /MANZ/ NZM, FM

Man-model external input parameters  $WOM=W_m^0$ ,  $EM=E_m$ ,  $FM=F_m$

15. /RATIOS/ PU, VU, PY, VY, TH, ATTN, SIGMA

Model parameters  $\rho_u$ ,  $v_u$ ,  $\rho_y$ ,  $v_y$ ,  $a$ ,  $f$ ,  $\Sigma_{k|k-1}$

16. /MANINC/ TD, NPRED, XHINC

Man-model parameters  $TD=\tau$ ,  $NPRED=[\tau/\Delta]=N$ ,  $XHINC=\delta \hat{p}$

17. /GAINBK/ CGN

CGN = discrete control gains  $L_d$  or equivalent discrete gains  $\hat{L}_d$  computed from  $L_c$

## 7. MCARLO LISTING

C NO TABS

C MCARLO - TIME VARYING MONTE CARLO MAN/MACHINE SIMULATION  
 INCLUDES  
 C 1 - BLOCK DATA MCDAT - INITIALIZES VARIOUS COMMON BLOCKS  
 C 2 - MAIN. - CALLS SUBROUTINE MCARLO  
 C 3 - SUBROUTINE MCARLO - PRIMARY SUBPROGRAM

C ALSO REQUIRES THE FOLLOWING SUBPROGRAM FILES

C MCCMP - COMPUTATIONS FOR MCARLO  
 INCLUDES  
 C 1 - SUBROUTINE SYSTM - PROPAGATES THE SYSTEM'S RESPONSE  
 C 2 - SUBROUTINE MAN - PROPAGATES THE MAN'S RESPONSE  
 C 3 - FUNCTION GAUSS - PICKS A NUMBER FROM A GAUSSIAN  
 C DISTRIBUTION

C MCP - PROBLEM DEPENDENT SUBPROGRAMS FOR MCARLO  
 INCLUDES  
 C 1 - SUBROUTINE FDET - GENERATES DETERMINISTIC INPUT  
 C 2 - SUBROUTINE SYSNEW - INTERNAL UPDATES TO THE SYSTEM  
 C 3 - SUBROUTINE MANNEW - INTERNAL UPDATES TO THE MAN

C MCIO - I/O FOR MCARLO  
 INCLUDES  
 C 1 - SUBROUTINE UPDATE - PERFORM EXTERNAL UPDATES  
 C 2 - SUBROUTINE INFORM - DO OUTPUT FOR A SINGLE TIME STEP  
 C 3 - SUBROUTINE PUTOUT - SAVES OUTPUT ON FILES  
 C 4 - SUBROUTINE PRINTR - PRINT THE OUTPUT AT THE END OF A RUN

C KPLOT - LINEPRINTER PLOTTING PACKAGE  
 INCLUDES  
 C 1 - SUBROUTINE KPLOT  
 C 2 - SUBROUTINE ADJUST  
 C 3 - SUBROUTINE QINIT  
 C 4 - SUBROUTINE KPOTC  
 C 5 - SUBROUTINE QPLOT  
 C 6 - SUBROUTINE PLACE  
 C 7 - SUBROUTINE QPRINT

C BLOCK DATA MCDAT  
 C INITIALIZES VARIOUS COMMON BLOCKS

COMMON  
 1 /INOU/ KIN, KOUT, KPTR, KPUNCH,  
 1 KDISK, IP0\$, IG0\$  
 2 /PLOT1/ NV, NH, NCPW, LW, XL, XH, YL, YH, NXES, NDIR, IST,  
 2 NGLV, NGLH, BSYM, GSYM, PSYM, ND1, ND2, NOUT

DATA  
 1 NV, NH, NXES, NDIR, NGLV, NGLH, BSYM, GSYM, PSYM, IST, ND1  
 1 / 51, 101, 1, 10, 20, 20, 1H+, 1H+, 1HX, 11, 1/

END

```
1 PROGRAM MCMAIN
2   (INPUT, OUTPUT, TAPE5=INPUT, TAPE6=OUTPUT,
3   DISK, POS, GOS, TAPE7=DISK, TAPE8=POS, TAPE9=GOS)
```

```
C      MAIN PROGRAM
C      CALLS SUBROUTINE MCARLO
```

```
      CALL MCARLO
      END
```

```

C      SUBROUTINE MCARLO
      PRIMARY SUBPROGRAM

      DIMENSION
1     TITLE(8),
2     X(30), Y(30), U(30), W(30), Z(30),
3     XMHAT(30), YMHAT(30), RES(30)

      COMMON
1     /INOU/   KIN, KOUT, KPTR, KPUNCH,
1           KDISK, IPOS, IGOS
2     /PLOT1/   NV, NH, NCPW, LW, XL, XH, YL, YH, NXES, NDIR, IST,
2           NGLV, NGLH, BSYM, GSYM, PSYM, ND1, ND2, NOUT
3     /MAIN1/   NDIM, NDIM1, COM1(15,15)
4     /MAIN2/   COM2(15,15), STORE(1800)
5     /TIMES/   TIME, DEL, TO, TEND, NPRNT
6     /INFO/    NREC, NPRINT, NPLOT, LPRNTS(60), LPRNTM(60),
6           IP(6), IG(6), SMIN(21), SMAX(21)
7     /FILES/   KKB, NAMIN, NAMOUT, NAMDYN, NAMPCH, NAMDSK,
7           NAMPOS, NAMGOS
Z     /COMP1/   X, Y, U, W, Z, XMHAT, YMHAT, RES

      DATA
1     KIN, KOUT, KPTR, NOUT /5, 6, 6, 6/
2     KPUNCH, KDISK, IPOS, IGOS /6, 7, 8, 9/

C      SET NDIM
NDIM=15
NDIM1=NDIM+1

C      WRITE DAYTIM
150   CALL PAGEFD(KOUT, 1)
      WRITE (KOUT, 1500)
1500  FORMAT (1H ,/,1H ,15HSTARTING MCARLO)
      CALL DAYTIM(KOUT)

C      ZERO THE VECTORS
200   DO 220 I=1,30
      X(I)=0.0
      Y(I)=0.0
      W(I)=0.0
      Z(I)=0.0
      U(I)=0.0
220   CONTINUE
      ISTEP=0

C      GET TITLE AND RANDOM NUMBER SEED
300   READ (KIN, 1040) (TITLE(I), I=1,8)
      IF (EOF(KIN)) 1000, 350
1040  FORMAT (8A10)
350   WRITE (KOUT, 1045) (TITLE(I), I=1,8)
1045  FORMAT (/,1H ,8A10,/,1H )
      READ (KIN, 1051) IDUM
1051  FORMAT (I10)
      WRITE (KOUT, 1052) IDUM
1052  FORMAT (21H RANDOM NUMBER SEED= ,I10)
      CALL RANSET(IDUM)

C      SPECIFY DEL, TO, TEND, AND NPRNT
330   READ (KIN, 1060) DEL, TO, TEND, NPRNT
1060  FORMAT (3E10.0,I10)
      TEND=IFIX((TEND-TO+0.0001)/DEL)*DEL+TO
      WRITE (KOUT, 1065) DEL, TO, TEND, NPRNT
1065  FORMAT (25H INTEGRATION TIME STEP = ,F10.3,/,
1           17H INITIAL TIME = ,F10.3,/,,

```

```
2 17H TERMINAL TIME = ,F10.3,/,  
3 22H PRINTOUT FREQUENCY = ,I5)  
  
C IDENTIFY VARIABLES FOR OUTPUT  
READ (KIN,1070) LPRNTS  
READ (KIN,1070) LPRNTM  
1070 FORMAT (6OI1)  
  
C SET THE TIME AND ENTER THE MAIN COMPUTATIONAL LOOP  
TIME=TO  
  
C START BY UPDATING THE SYSTEM  
600 CALL SYSTM(TIME,X,Y,U,W,Z)  
C RETURNS X,Y AT T, GIVEN U,W,Z OVER (T-DEL,T)  
  
C UPDATE THE MAN  
CALL MAN(IDUM,Y,U,Z,XMHAT,YMHAT,RES)  
C RETURNS U OVER (T,T+DEL) GIVEN Y AT T  
  
C CALL INFORM TO DO A PRINTOUT IF ONE IS DUE AT THIS TIME  
CALL INFORM(ISTEP,X,Y,U,XMHAT,YMHAT,RES)  
  
C UPDATE THE TIME  
ISTEP=ISTEP+1  
TIME=DEL*ISTEP+TO  
C IF THE TIME IS NOT EXPIRED DO ANOTHER ITERATION  
IF (TIME+0.0001 .GE. TEND) GO TO 800  
GO TO 600  
  
C TIME IS EXPIRED. DO OUTPUT AND START AGAIN  
800 CALL PRINTR(NPRINT,NPLOT,X,Z)  
GO TO 200  
  
C INPUT FILE IS EMPTY  
C WRITE MESSAGE AND EXIT  
1000 WRITE (KOUT,9000)  
9000 FORMAT (1H ,15HSTOPPING MCARLO)  
CALL EXIT  
  
END
```

```

C      MCCMP - COMPUTATIONS FOR MCARLO
C      INCLUDES
C          1 - SUBROUTINE SYSTM
C          2 - SUBROUTINE MAN
C          3 - FUNCTION GAUSS

C      SUBROUTINE SYSTM(T,X,Y,U,W,Z)
C      INTEGRATES SYSTEM EQUATIONS ONE TIME STEP
C      HANDLES EXTERNAL AND INTERNAL SYSTEM UPDATES
C      THIS VERSION IS FOR A LINEAR SYSTEM USING TRANSITION MATRIX
C      PROPAGATION
C      A MORE GENERAL VERSION WOULD USE RUNGE-KUTTA.

C      DIMENSION
1     X(30), Y(30), U(30), W(30), Z(30),
2     DUM(20), NSTEP(10), ISFLAG(16), AINT(15,15), MDUM(16),
3     XMEAN(30), YMEAN(30), UMEAN(30),
4     XRMS(30), YRMS(30), URMS(30)

C      INTEGER
1     NSCODE(10)

C      COMMON
1     /INOU/   KIN, KOUT, KPTR, KPUNCH,
1           KDISK
5     /TIMES/   TIME, DEL, TO, TEND, NPRNT
8     /SYSX/    NX, NU, BS(15,4), AS(15,15)
9     /SYSAD/   BD(15,4), AD(15,15)
A     /SYSY/    NY, DS(15,4), CS(15,15)
B     /SYSW/    NW, WO(4), ES(15,4)
C     /SYSZ/    NZ, FS(15,4)
D     /SYSINC/  XINC(15)

C      DATA
1     NSCODE, LTIME, LEND
1     /10, 4HTIME, 4HENDS/,
2     NSCODE
2     /1HA, 1HB, 1HC, 1HD, 1HE,
2     1HF, 2HWO, 4HXINC, 3HINT, 5HPRINT/

C      IF (T .GT. TO+0.0001) GO TO 100

C      INITIALIZATION
C      SPECIFY THE SYSTEM INTERNAL BREAKS
1050  READ (KIN,1050) (NSTEP(I), I=1,NSCODE)
      FORMAT (16I5)
      WRITE (KOUT,1060)
1060  FORMAT (24H SYSTEM INTERNAL BREAKS ,17H INDEX CODE NDT)
      DO 65 I=1,NSCODE
      IF (NSTEP(I) .LE. 0) GO TO 65
      WRITE (KOUT,1070) I, NSCODE(I), NSTEP(I)
1070  FORMAT (28X,I2,3X,A5,1X,15)
      65 CONTINUE

C      WRITE THE NEXT BATCH OF INPUT CARDS UNTIL AN 'END' CARD
      REWIND KDISK
72      READ (KIN,1075) MDUM
1075  FORMAT (16A5)
      WRITE (KDISK,1075) MDUM
      II=MDUM(1)
      IF (II.EQ.LEND) GO TO 80
      GO TO 72
      TNEXT=TO
      REWIND KDISK
      KIN1=KIN

```

```

C      IXYZ=35617
      INITIALIZE SOME MORE QUANTITIES
      NW=0
      NZ=0
      DO 85 I=1,15
      XINC(I)=0.0
      DO 85 J=1,4
      DS(I,J)=0.0
85    CONTINUE
      RNPTS=DEL/(TEND-TO)
      DO 90 I=1,30
      XMEAN(I)=0.0
      YMEAN(I)=0.0
      UMEAN(I)=0.0
      XRMS(I)=0.0
      YRMS(I)=0.0
      URMS(I)=0.0
90    CONTINUE

C      TAKE CARE OF INTERNAL SYSTEM BREAKS
100    DO 105 I=1,NSCODE
           ISFLAG(I)=0
           IF (NSTEP(I) .EQ. 0) GO TO 105
           ITME=IFIX((T-TO+0.0001)/DEL)
           IF (MOD(ITME,NSTEP(I)) .EQ. 0) CALL SYSNEW(I)
105    CONTINUE

C      TAKE CARE OF EXTERNAL SYSTEM BREAKS
110    IF (T+0.0001 .LT. TNEXT) GO TO 500
120    READ (KDISK,1130) IDEN, NQQ, BRKT
1130   FORMAT (A5,2X,I3,E10.0)
           IF (IDEN.NE.LEND) GO TO 140
135    TNEXT=1.0E+05
           GO TO 110
140    IF (IDEN .NE. LTIME) GO TO 150
           TNEXT=BRKT
           GO TO 110

C      SEARCH THROUGH THE UPDATE CODES, SCODE(KEY)
150    DO 160 KEY=1,NSCODE
           IF (IDEN.EQ.SCODE(KEY)) GO TO 170
160    CONTINUE

C      CODE WAS ILLEGAL
1165   WRITE (KOUT,1165) IDEN
           FORMAT (23H ILLEGAL INPUT CODE OF ,A5)
           CALL EXIT

C      DO THE SPECIFIED SYSTEM EXTERNAL UPDATE
170    ISFLAG(KEY)=1
           IO=2
           KIN=KDISK
           WRITE (KOUT,1175) TIME, IDEN, NQQ
1175   1 FORMAT (/28H SYSTEM EXTERNAL BREAK AT T= ,F8.3,4X,4HCODE,2X,A5,
           4X,7HINDEX= ,I3)
           GO TO (1,2,3,4,5,6,7,8,9,10), KEY

C      SYSTEM DYNAMICS - A, B, C, D, E
1      NX=NQQ
           CALL MATIO(AS,NX,NX,IO)
           GO TO 120
2      NU=NQQ
           CALL MATIO(BS,NX,NU,IO)
           GO TO 120
3      NY=NQQ
           CALL MATIO(CS,NY,NX,IO)

```

```

        GO TO 120
4      NY=NQQ
        CALL MATIO(DS,NY,NU,IO)
        GO TO 120
5      NW=NQQ
        IF (NW.GT.0) CALL MATIO(ES,NX,NW,IO)
        GO TO 120

C      DETERMINISTIC INPUT (F MATRIX) - F
6      NZ=NQQ
        IF (NZ.GT.0) CALL MATIO(FS,NX,NZ,IO)
        GO TO 120

C      DRIVING NOISE - W0
7      NW=NQQ
        IF (NW.GT.0) CALL VECTIO(W0,NW,IO)
        GO TO 120

C      INCREMENT TO STATES - XINC
8      CALL VECTIO(XINC,NX,IO)
        GO TO 120

C      CALL AN INTERNAL UPDATE - INT
9      CALL SYSNEW(NQQ)
        GO TO 120

C      SET PRINT INTERVAL - PRINT
10     NPRNT=NQQ
        GO TO 120

C      NO MORE SYSTEM EXTERNAL UPDATES AT THIS TIME
500    KIN=KIN1

C      COMPUTE DISCRETE SYSTEM MATRICES
        IF (ISFLAG(1) .EQ. 0) GO TO 510
        CALL DSCRT(NX,AS,DEL,AD,AINT,5}
510    IF (ISFLAG(1)+ISFLAG(2) .EQ. 0) GO TO 520
        CALL MMUL(AINT,BS,NX,NX,NU,BD)
520    IF (ISFLAG(8) .EQ. 0) GO TO 540
        DO 530 I=1,NX
        X(I)=X(I)+XINC(I)
530    CONTINUE

C      COMPUTATION OF TIME AVERAGES
540    IF (T .LT. T0+0.0001) GO TO 630
        DO 550 I=1,NX
        XMEAN(I)=XMEAN(I)+X(I)*RNPTS
        XRMS(I)=XRMS(I)+(X(I)**2)*RNPTS
550    CONTINUE
        DO 560 I=1,NY
        YMEAN(I)=YMEAN(I)+Y(I)*RNPTS
        YRMS(I)=YRMS(I)+(Y(I)**2)*RNPTS
560    CONTINUE
        DO 570 I=1,NU
        UMEAN(I)=UMEAN(I)+U(I)*RNPTS
        URMS(I)=URMS(I)+(U(I)**2)*RNPTS
570    CONTINUE

C      COMPUTE XRMS, YRMS URMS AT THE END OF THE RUN
        IF (TIME+DEL+0.0001 .LT. TEND) GO TO 590
        DO 575 I=1,NX
        XRMS(I)=SQRT(XRMS(I)-XMEAN(I)**2)
575    CONTINUE
        DO 580 I=1,NY
        YRMS(I)=SQRT(YRMS(I)-YMEAN(I)**2)
580    CONTINUE

```

```

      DO 585 I=1,NU
      URMS(I)=SQRT(URMS(I)-UMEAN(I)**2)
585    CONTINUE

C      OUTPUT THE MEAN AND RMS VALUES OF THE X, Y AND U VECTORS
      IO=3
      WRITE (KOUT,2000)
2000   FORMAT (17H MEAN OF X VECTOR)
      CALL VECTIO(XMEAN,NX,IO)
      WRITE (KOUT,2010)
2010   FORMAT (23H RMS VALUES OF X VECTOR)
      CALL VECTIO(XRMS,NX,IO)
      WRITE (KOUT,2020)
2020   FORMAT (17H MEAN OF Y VECTOR)
      CALL VECTIO(YMEAN,NY,IO)
      WRITE (KOUT,2030)
2030   FORMAT (23H RMS VALUES OF Y VECTOR)
      CALL VECTIO(YRMS,NY,IO)
      WRITE (KOUT,2040)
2040   FORMAT (17H MEAN OF U VECTOR)
      CALL VECTIO(UMEAN,NU,IO)
      WRITE (KOUT,2050)
2050   FORMAT (23H RMS VALUES OF U VECTOR)
      CALL VECTIO(URMS,NU,IO)

C      INTEGRATE SYSTEM EQUATIONS
590    DO 600 I=1,NX
      DUM(I)=0.0
600    CONTINUE
      IF (NW .GT. 0) CALL VMAT2(DUM,ES,W,NX,NW,DUM)
      IF (NZ .GT. 0) CALL VMAT2(DUM,FS,Z,NX,NZ,DUM)
      DO 605 I=1,NX
      DUM(I)=DUM(I)*DEL
605    CONTINUE
      CALL VMAT2(DUM,AD,X,NX,NX,DUM)
      CALL VMAT2(DUM,BD,U,NX,NU,X)
      CALL VMAT1(CS,X,NY,NX,DUM)
      CALL VMAT2(DUM,DS,U,NY,NU,Y)

C      X(T+DEL) AND Y(T+DEL) HAVE JUST BEEN COMPUTED
C      NOW OBTAIN W AND Z OVER (T,T+DEL) FOR THE NEXT STEP
630    IF (T+0.0001 .GE. TEND) GO TO 650
      IF (NW .EQ. 0) GO TO 640
      DO 635 I=1,NW
      C1=SQRT(W0(I)/DEL)
      W(I)=GAUSS(IXYZ)*C1
635    CONTINUE
      IF (NZ .EQ. 0) GO TO 650
      DO 645 I=1,NZ
      Z(I)=FDET(I,T)
645    CONTINUE
      RETURN

      END

```

```

C      SUBROUTINE MAN(IDUM,Y,U,Z,XH,YHAT,RES)
C      INTEGRATES MAN EQUATIONS ONE TIME STEP
C      CALLS SUBROUTINES FOR EXTERNAL AND INTERNAL MAN UPDATES

DIMENSION
1      Y(30), U(30), Z(30), PASTY(15,11), P(30), XH(30), YHAT(30),
2      VU0(4), RES(30), IMFLAG(32), AVGY2(30), AVGU(4), AVGU2(4),
3      VY0(30), FGAIN(15,15), PASTUC(4,11)

COMMON
1      /INOU/   KIN, KOUT, KPTR, KPUNCH,
1          KDISK, IP0S, IG0S
3      /MAIN1/  NDIM, NDIM1, COM1(1)
4      /MAIN2/  COM2(1)
5      /TIMES/   TIME, DEL, TO, TEND, NPRNT
E      /MANX/    NXM, NUM, BM(15,4), AM(225)
F      /MANAD/   BD(15,4), AD(15,15)
G      /MANY/    NYM, DM(15,4), CM(225)
H      /MANW/    NWM, WOM(8), EM(60)
I      /MANZ/    NZM, FM(60)
J      /MANINC/  TD, NPRED, XHINC(30)
K      /RATIOS/  PU(30), VU(30), PY(30), VY(30), TH(30), ATTN(30),
K          SIGMA(15,15)
L      /GAINBK/  CGN(225)

C      INITIALIZE VECTORS AND MATRICES IF TIME IS LESS THAN TO
IF (TIME .GT. TO+0.0001) GO TO 100
DO 10 I=1,30
P(I)=0.0
XH(I)=0.0
YHAT(I)=0.0
RES(I)=Y(I)
AVGY2(I)=Y(I)*Y(I)
10    CONTINUE
DO 12 I=1,4
DO 11 J=1,11
PASTUC(I,J)=0.0
11    CONTINUE
VU0(I)=0.0
AVGU(I)=0.0
AVGU2(I)=0.0
12    CONTINUE
KOUNT=0
CALL IDENT(NDIM,SIGMA,1.0E-05)
TCOR=1.0
TMEM=0.5
ALPHA=EXP(-DEL/TMEM)
TPR=TMEM
DO 13 I=1,15
DO 13 J=1,11
PASTY(I,J)=Y(I)
13    CONTINUE

C      DO EXTERNAL AND INTERNAL MAN UPDATES
100   CALL UPDATE(IMFLAG)
NTOT=NXM+NUM
IF (IMFLAG(8) .EQ. 1) CALL VADD(NXM,1.0,P,XHINC)
TPR=TPR*ALPHA+DEL
LOC=NPRED+1
DO 110 I=1,NYM
PASTY(I,LOC)=Y(I)
C2=PASTY(I,1)
AVGY2(I)=ALPHA*AVGY2(I)+C2*C2*DEL
C1=ABS(C2)
C1=XGAIN(TH(I),0.0,C1)
C3=C1*C1*ATTN(I)

```

```

C1=PY(I)
IF (KOUNT .LT. NPRED) C1=1.0E+10
VY0(I)=(C2*C2*C1+VY(I))/C3
RES(I)=SQRT(VY0(I)/DEL)*GAUSS(IDUM)+C2
RES(I)=RES(I)-DOT3(NTOT,CM(I),P)
VY0(I)=(AVGY2(I)*C1/TPR+VY(I))/C3
110 CONTINUE

C UPDATE THE KALMAN FILTER ESTIMATES
CALL MMUL(CM,SIGMA,NYM,NTOT,NTOT,COM1)
CALL MAT2(NYM,NTOT,COM1,CM,FGAIN)
DO 120 I=1,NYM
FGAIN(I,I)=FGAIN(I,I)+VY0(I)/DEL
120 CONTINUE
CALL GMINV(NYM,NYM,FGAIN,COM2,M RANK,0)
CALL MAT5A(COM1,COM2,NTOT,NYM,NYM,FGAIN)
CALL VMAT2(P,FGAIN,RES,NTOT,NYM,P)
CALL MMUL(FGAIN,CM,NTOT,NYM,NTOT,COM2)
CALL DIAG2(NTOT,COM2,COM2,-1.0,1.0)
CALL MMUL(COM2,SIGMA,NTOT,NTOT,NTOT,COM1)
DO 130 I=1,NYM
C1=VY0(I)/DEL
DO 130 J=1,NTOT
SIGMA(J,I)=C1*FGAIN(J,I)
130 CONTINUE
CALL MAT2(NTOT,NYM,FGAIN,SIGMA,SIGMA)
CALL MAT6S(NTOT,NTOT,COM1,COM2,SIGMA)

C OBTAIN PREDICTION OF CURRENT STATE
DO 140 I=1,NTOT
YHAT(I)=0.0
XH(I)=P(I)
140 CONTINUE
IF (NPRED.EQ.0) GO TO 170
LOC1=NPRED+1
DO 150 L=1,NPRED
CALL VMAT1(AD,XH,NTOT,NTOT,YHAT)
CALL VMAT2(YHAT,BD,PASTUC(1,L),NTOT,NUM,XH)
150 CONTINUE
170 CALL VMAT1(CGN,XH,NUM,NXM,PASTUC(1,LOC))
DEL2=-0.5*DEL
DO 172 I=1,NUM
C1=ABS(VUO(I))
PASTUC(I,LOC)=DEL2*PASTUC(I,LOC)
YHAT(I)=DEL2*(U(I)+SQRT(C1/DEL)*GAUSS(IDUM))
U(I)=U(I)+PASTUC(I,LOC)
WOM(I+NWM)=C1
II=NDIM*NXM+1
CALL VMAT2(U,CGN(II),YHAT,NUM,NUM,U)
DO 175 I=1,NUM
AVGU(I)=ALPHA*AVGU(I)+U(I)*DEL
AVGU2(I)=ALPHA*AVGU2(I)+U(I)*U(I)*DEL
C1=AVGU(I)/TPR
VUO(I)=(AVGU2(I)/TPR-C1*C1)*PU(I)+VU(I)
175 CONTINUE

C PROPAGATE SIGMA, P
CALL VMAT1(AD,P,NTOT,NTOT,YHAT)
CALL VMAT2(YHAT,BD,PASTUC,NTOT,NUM,P)
CALL VMAT1(CM,XH,NYM,NTOT,YHAT)
CALL MMUL(AD,SIGMA,NTOT,NTOT,NTOT,COM1)
NWU=NWM+NUM
II=1
DO 200 I=1,NWU
C1=WOM(I)*DEL
CALL VSCALE(COM2(II),EM(II),NTOT,C1)

```

```
200      II=II+NDIM
        CONTINUE
        CALL MAT2(NTOT,NWU,COM2,EM,SIGMA)
        IF (NZM.EQ.0) GO TO 220
        II=1
        DO 210 I=1,NZM
        C1=Z(I)*Z(I)*TCOR*DEL
        CALL VSCALE(COM2(II),FM(II),NXM,C1)
        II=II+NDIM
210      CONTINUE
        CALL MAT6S(NXM,NZM,COM2,FM,SIGMA)
220      CALL MAT6S(NTOT,NTOT,COM1,AD,SIGMA)
        IF (NPRED.EQ.0) GO TO 235
        CALL EQUATE(PASTY,PASTY(1,2),NYM,NPRED)
        DO 230 I=1,NPRED
        DO 230 J=1,NUM
        PASTUC(J,I)=PASTUC(J,I+1)
        CONTINUE
230      KOUNT=KOUNT+1
        IF (KOUNT.GT.NPRED) KOUNT=NPRED
235      RETURN

C      DUMMY CALL TO MAT6 TO FORCE LOADING
        CALL MAT6(NTOT,NTOT,COM1,COM1,COM1)

        END
```

```
C FUNCTION GAUSS(DUM)
C RETURNS A GAUSSIAN RANDOM VARIABLE
C WITH ZERO MEAN AND UNIT STD DEVIATION
C BY SUMMING 12 UNIFORMLY DISTRIBUTED VARIABLES
A=0.0
DO 50 I=1,12
A=A+RANF(DUM)
CONTINUE
GAUSS=A-6.0
RETURN
50
END
```

```

C      MCIO - I/O FOR MCARLO
C      INCLUDES
C          1 - SUBROUTINE UPDATE
C          2 - SUBROUTINE INFORM
C          3 - SUBROUTINE PUTOUT
C          4 - SUBROUTINE PRINTR

C      SUBROUTINE UPDATE(IMFLAG)
C      PERFORM EXTERNAL UPDATES TO THE MAN

DIMENSION
1 IMFLAG(20), MCODE(20), NSTEP(32)

COMMON
1 /INOU/    KIN, KOUT, KPTR, KPUNCH,
1           KDISK
3 /MAIN1/   NDIM, NDIM1, COM1(1)
5 /TIMES/   TIME, DEL, TO, TEND, NPRNT
8 /SYSX/    NX, NU, B(15,4), A(1)
A /SYSY/    NY, D(15,4), C(1)
B /SYSW/    NW, WO(4), E(1)
C /SYSZ/    NZ, F(1)
E /MANX/    NXM, NUM, BM(15,4), AM(15,15)
F /MANAD/   BD(15,4), AD(15,15)
G /MANY/    NYM, DM(15,4), CM(15,15)
H /MANW/    NWM, WOM(8), EM(15,4)
I /MANZ/    NZM, FM(15,4)
J /MANINC/  TD, NPRED, XHINC(30)
K /RATIOS/  PU(30), VU(30), PY(30), VY(30), TH(30), ATTN(30),
K           SIGMA(15,15)
L /GAINBK/  CGN(15,15)

DATA
1 NMPCODE, LEND, PI, LTIME
1 /20, 4HENDM, 3.14159, 4HTIME/, 
2 MCODE
2 /2HAM, 2HBM, 2HCM, 2HDM, 2HEM, 2HFM, 3HWOM, 5HXHINC,
2 2HTD, 3HMNA, 3HMNR, 3HSNA, 3HSNR, 2HTH, 4HATTN,
2 5HCGAIN, 5HDGAIN, 3HINT, 5HPRINT, 5HDUMMY/

IF (TIME .GT. TO+0.0001) GO TO 100

INITIALIZATION
SPECIFY THE MAN INTERNAL BREAKS
READ (KIN,1050) (NSTEP(I), I=1,NMPCODE)
1050 FORMAT (16I5)
WRITE (KOUT,1060)
1060 FORMAT (23H HUMAN INTERNAL BREAKS ,17H INDEX CODE NDT)
DO 65 I=1,NMPCODE
IF (NSTEP(I) .LE. 0) GO TO 65
WRITE (KOUT,1070) I, MCODE(I), NSTEP(I)
1070 FORMAT (27X,I2,3X,A5,1X,I5)
65 CONTINUE

PARAMETER INITIALIZATION
TNEXT=TO
DO 80 I=1,30
PU(I)=0.0
XHINC(I)=0.0
VU(I)=0.0
PY(I)=0.0
VY(I)=0.0
TH(I)=0.0
ATTN(I)=1.0
80 CONTINUE

```

```

NPRED=0
DO 85 I=1,NDIM
DO 85 J=1,4
DM(I,J)=0.0
85 CONTINUE
TD=0.0
NWM=0
NZM=0

C   TAKE CARE OF INTERNAL MAN BREAKS
100 DO 105 I=1,NMCODE
IMFLAG(I)=0
IF (NSTEP(I) .EQ. 0) GO TO 105
ITME=IFIX((TIME-T0+0.0001)/DEL)
IF (MOD(ITME,NSTEP(I)) .EQ. 0) CALL MANNEW(I)
105 CONTINUE

C   TAKE CARE OF EXTERNAL MAN BREAKS
110 IF (TIME+0.0001 .LT. TNEXT) GO TO 500
120 READ (KIN,1130) IDEN, NQQ, BRKT
1130 FORMAT (A5,2X,I3,E10.0)
IF (IDEN.NE.LEND) GO TO 140
135 TNEXT=1.0E+05
GO TO 110
140 IF (IDEN.NE.LTIME) GO TO 150
TNEXT=BRKT
GO TO 110

C   SEARCH THROUGH THE UPDATE CODES
150 DO 160 KEY=1,NMCODE
IF (IDEN.EQ.MCODE(KEY)) GO TO 170
160 CONTINUE

C   CODE WAS ILLEGAL
1165 WRITE (KOUT,1165) IDEN
FORMAT (23H ILLEGAL INPUT CODE OF ,A5)
CALL EXIT

C   DO THE SPECIFIED MAN EXTERNAL UPDATE
170 IMFLAG(KEY)=1
WRITE (KOUT,1175) TIME, IDEN, NQQ
1175 1 FORMAT (/,27H HUMAN EXTERNAL BREAK AT T= ,F8.3,4X,4HCODE,2X,A5,
4X,7HINDEX= ,I3)
IF (NQQ.LE.0 .AND. KEY.LE.7) WRITE (KOUT,1180)
FORMAT (21H HUMAN MODEL = SYSTEM)
IO=2
GO TO (1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19), KEY

C   SYSTEM DYNAMICS - AM, BM, CM, DM, EM
1 NXM=NQQ
IF (NXM.LE.0) GO TO 201
CALL MATIO(AM,NXM,NXM,IO)
GO TO 120
201 NXM=NX
CALL EQUATE(AM,A,NXM,NXM)
GO TO 120
2 NUM=NQQ
IF (NUM.LE.0) GO TO 202
CALL MATIO(BM,NXM,NUM,IO)
GO TO 120
202 NUM=NU
CALL EQUATE(BM,B,NXM,NUM)
GO TO 120
3 NYM=NQQ
IF (NYM.LE.0) GO TO 203
CALL MATIO(CM,NYM,NXM,IO)

```

```

GO TO 120
203  NYM=NY
      CALL EQUATE(CM,C,NYM,NXM)
      GO TO 120
4     NYM=NQQ
      IF (NYM.LE.0) GO TO 204
      CALL MATIO(DM,NYM,NUM,IO)
      GO TO 120
204  NYM=NY
      CALL EQUATE(DM,D,NYM,NXM)
      GO TO 120
5     NWM=NQQ
      IF (NWM.LE.0) GO TO 205
      CALL MATIO(EM,NXM,NWM,IO)
      GO TO 120
205  NWM=NW
      IF (NW.GT.0) CALL EQUATE(EM,E,NXM,NWM)
      GO TO 120

C   DETERMINISTIC INPUT (FM MATRIX) - FM
6     NZM=NQQ
      IF (NZM.LE.0) GO TO 206
      CALL MATIO(FM,NXM,NZM,IO)
      GO TO 120
206  NZM=NZ
      IF (NZ.GT.0) CALL EQUATE(FM,F,NXM,NZM)
      GO TO 120

C   DRIVING NOISE - WOM
7     NWM=NQQ
      IF (NWM.LE.0) GO TO 207
      CALL VECTIO(WOM,NWM,IO)
      GO TO 120
207  NWM=NW
      IF (NW.GT.0) CALL EQUATE(WOM,W0,NWM,1)
      GO TO 120

C   INCREMENT TO STATE ESTIMATES - XHINC
8     CALL VECTIO(XHINC,NXM,IO)
      GO TO 120

C   TIME DELAY - TD
9     CALL VECTIO(TD,1,IO)
      NPRED=IFIX(TD/DEL+0.5001)
      TD=DEL*NPRED
      GO TO 120

C   NOISES - MNA, MNR, SNA, SNR
10    CALL VECTIO(VU,NUM,IO)
      GO TO 120
11    CALL VECTIO(PU,NUM,IO)
      DO 211 I=1,NUM
      PU(I)=PI*10.0**((PU(I)/10.0))
211    CONTINUE
      GO TO 120
12    CALL VECTIO(VY,NYM,IO)
      GO TO 120
13    CALL VECTIO(PY,NYM,IO)
      DO 213 I=1,NYM
      PY(I)=PI*10.0**((PY(I)/10.0))
213    CONTINUE
      GO TO 120

C   THRESHOLDS AND ATTENTION - TH, ATTN
14    CALL VECTIO(TH,NYM,IO)
      GO TO 120

```

```

15      CALL VECTIO(ATTN,NYM,IO)
          GO TO 120

C      CONTINUOUS AND DISCRETE CONTROL GAINS - CGAIN, DGAIN
16      CALL MATIO(CGN,NUM,NUM+NXM,IO)
          GO TO 120
17      CALL MATIO(CGN,NUM,NUM+NXM,IO)
          GO TO 120

C      CALL AN INTERNAL MAN UPDATE - INT
18      CALL MANNEW(NQQ)
          GO TO 120

C      PRINT INTERVAL - PRINT
19      NPRNT=NQQ
          GO TO 120

C      NO MORE MAN UPDATES AT THIS TIME
500     CONTINUE
C      UPDATE VARIOUS MAN PARAMETERS
      NTOT=NXM+NUM
C      COMPUTE DISCRETE MAN MATRICES
      IF (IMFLAG(1)+IMFLAG(2) .EQ. 0) GO TO 520
      DO 510 I=1,NUM
      II=NXM+I
      DO 505 J=1,NXM
      AD(II,J)=0.0
505     CONTINUE
      DO 506 K=1,NUM
      BD(II,K)=0.0
506     CONTINUE
      BD(II,I)=1.0
510     CONTINUE
      CALL DSCRT(NXM,AM,DEL,AD,COM1,5)
      CALL MMUL(COM1,BM,NXM,NXM,NUM,BD)
      CALL EQUATE(AM(1,NXM+1),BM,NXM,NUM)

C      INCORPORATE NEW CGAINS
520     IF (IMFLAG(16).EQ.0) GO TO 540
      CALL MSCALE(AM(NXM+1,1),CGN,NUM,NTOT,-1.0)
      CALL DSCRT(NTOT,AM,DEL,CGN,COM1,5)
      CALL MMUL(AM(NXM+1,1),COM1,NUM,NTOT,NTOT,CGN)
      DO 525 I=1,NUM
      II=I+NXM
      DO 525 J=1,NTOT
      AM(II,J)=0.0
      CGN(I,J)=-CGN(I,J)/DEL
525     CONTINUE
      WRITE (KOUT,5250)
5250    FORMAT (37H EQUIVALENT DISCRETE GAINS GENERATED )
      IO=3
      CALL MATIO(CGN,NUM,NTOT,IO)

C      UPDATE EM AND CM
540     CALL MMUL(BD,CGN(1,NXM+1),NTOT,NUM,NUM,EM(1,NWM+1))
      CALL EQUATE(CM(1,NXM+1),DM,NYM,NUM)
      DO 550 J=1,NUM
      JJ=J+NXM
      JQ=J+NWM
      DO 550 I=1,NTOT
      EM(I,JQ)=0.5*EM(I,JQ)
      AD(I,JJ)=BD(I,J)-DEL*EM(I,JQ)
550     CONTINUE
      IF (IMFLAG(5)+IMFLAG(7).EQ.0) GO TO 570
      IQ=NXM+1
      IF (NWM.LE.0) GO TO 570

```

DO 560 J=1,NWM  
DO 560 I=IQ,NTOT  
560 EM(I,J)=0.0  
570 CONTINUE  
RETURN  
END

```

C      SUBROUTINE INFORM(ISTEP,X,Y,U,XH,YH,RES)
C      DO OUTPUT FOR A SINGLE TIME STEP

1      DIMENSION X(1), Y(1), U(1), XH(1), YH(1), RES(1), DUM1(21), DUM2(21)

1      COMMON /INOU/ KIN, KOUT, KPTR, KPUNCH,
1                  KDISK, IPOS, IGOS
1
5      /TIMES/   TIME, DEL, TO, TEND, NPRINT
6      /INFO/    NREC, NPRINT, NPLOT, LPP(20,6), IP(6), IG(6),
6                  SMIN(21), SMAX(21)

C      CHECK IF TIME FOR SOME OUTPUT
C      IF (MOD(ISTEP,NPRINT) .NE. 0) RETURN

C      DO SOME INITIALIZATION
C      IF (TIME .GT. TO+0.0001) GO TO 100
C      NPRINT=1
C      NPLOT=1
C      REWIND IPOS
C      REWIND IGOS
C      DO 8 I=1,21
C          SMIN(I)=1.0E+20
C          SMAX(I)=-1.0E+20
8      CONTINUE
C      DO 10 I=1,6
C          IP(I)=0
C          IG(I)=0
C      DO 9 J=1,20
C          L1=LPP(J,I)
C          IF (L1.EQ.1 .OR. L1.EQ.2) IP(I)=IP(I)+1
C          IF (L1.EQ.2 .OR. L1.EQ.3) IG(I)=IG(I)+1
9      CONTINUE
C      NPRINT=NPRINT+IP(I)
C      NPLOT=NPLOT+IG(I)
10     CONTINUE
C      NREC=0
C      IF (ISTEP.EQ.0) RETURN

C      DO OUTPUT FOR THE CURRENT TIME
100    DUM1(1)=TIME
C      DUM2(1)=TIME
C      IF (SMIN(1).GE.TIME) SMIN(1)=TIME
C      SMAX(1)=TIME
C      LOC1=1
C      LOC2=1
C      DO 160 J=1,6
C          DO 160 I=1,20
C              L1=LPP(I,J)
C              IF (L1.GE.3) GO TO 140
C              IF (L1.LE.0) GO TO 160
C              LOC1=LOC1+1
C              IF (J.EQ.1) DUM1(LOC1)=X(I)
C              IF (J.EQ.2) DUM1(LOC1)=Y(I)
C              IF (J.EQ.3) DUM1(LOC1)=U(I)
C              IF (J.EQ.4) DUM1(LOC1)=XH(I)
C              IF (J.EQ.5) DUM1(LOC1)=YH(I)
C              IF (J.EQ.6) DUM1(LOC1)=RES(I)
140    IF (L1.EQ.1) GO TO 160
C              LOC2=LOC2+1
C              IF (J.EQ.1) DUM2(LOC2)=X(I)
C              IF (J.EQ.2) DUM2(LOC2)=Y(I)
C              IF (J.EQ.3) DUM2(LOC2)=U(I)
C              IF (J.EQ.4) DUM2(LOC2)=XH(I)
C              IF (J.EQ.5) DUM2(LOC2)=YH(I)

```

```
150    IF (J.EQ.6) DUM2(LOC2)=RES(I)
      C1=DUM2(LOC2)
      IF (SMIN(LOC2).GE.C1) SMIN(LOC2)=C1
      IF (SMAX(LOC2).LE.C1) SMAX(LOC2)=C1
160    CONTINUE
      IF (LOC1.GT.1) CALL PUTOUT(DUM1,NPRINT,IPOS)
      IF (LOC2.GT.1) CALL PUTOUT(DUM2,NPLOT,IGOS)
      NREC=NREC+1
      RETURN
END
```

```
C      SUBROUTINE PUTOUT(DUM,NVAR,IDISK)
C      SUBROUTINE TO SAVE OUTPUT ON A FILE
1      DIMENSION
      DUM(1)
      WRITE (IDISK) (DUM(I), I=1,NVAR)
      RETURN
      END
```

```

C      SUBROUTINE PRINTR(NPRINT,NPLOT,DUM1,DUM2)
      PRINT THE OUTPUT AT THE END OF A RUN

      DIMENSION
      1 DUM1(1), DUM2(1), GRAPH(1350), TITLE(6), LET(11)

      COMMON
      1 /INOU/   KIN, KOUT, KPTR, KPUNCH,
      1       KDISK, IP0S, IGOS
      2 /PLOT1/   NV, NH, NCPW, LW, XL, XH, YL, YH, NXES, NDIR, IST,
      2       NGLV, NGLH, BSYM, GSYM, PSYM, ND1, ND2, NOUT
      3 /MAIN1/   NDIM, NDIM1, STORE(1)
      4 /MAIN2/   COM2(1)
      6 /INFO/    NREC, I1, I2, LPP(20,6), IP(6), IG(6),
      6       SMIN(21), SMAX(21)

      DATA
      1 TITLE
      1 /8H STATE , 8H OUTPUT , 8H CONTROL , 8H XMHAT ,
      1     8H YMHAT , 8H INOVAT /

      IF (NPRINT.EQ.1) GO TO 51
      REWIND IP0S
      DO 10 I=1,NREC
      READ (IP0S) (DUM1(KK), KK=1,NPRINT)
      II=I
      DO 9 L=1,NPRINT
      STORE(II)=DUM1(L)
      II=II+NREC
      9 CONTINUE

      IBEG=NREC+1
      DO 50 I=1,6
      M=0
      DO 30 L=1,20
      IQ=LPP(L,I)
      IF (IQ.EQ.0 .OR. IQ.EQ.3) GO TO 30
      M=M+1
      LET(M)=L
      30 CONTINUE
      IF (M.EQ.0) GO TO 50
      CALL PAGEFD(KOUT,1)
      WRITE (KOUT,1035) (TITLE(I), LET(J),J=1,M)
      1035 FORMAT (1H ,3X,4HTIME,2X,10(A8,I2,2X))
      LIM1=IBEG
      LIM2=IBEG+(M-1)*NREC
      DO 40 L=1,NREC
      WRITE (KOUT,1045) STORE(L), (STORE(J), J=LIM1,LIM2,NREC)
      1045 FORMAT (1H ,F7.2,10(2X,1PE10.3))
      LIM1=LIM1+1
      LIM2=LIM2+1
      40 CONTINUE
      50 IBEG=IBEG+M*NREC

      51 IF (NPLOT.EQ.1) RETURN
      REWIND IGOS

      DO 60 I=1,NREC
      READ (IGOS) (DUM2(KK),KK=1,NPLOT)
      II=I
      DO 59 L=1,NPLOT
      STORE(II)=DUM2(L)
      II=II+NREC
      59 CONTINUE
      60

```

```
ND2=NREC
XH=SMAX(1)
XL=SMIN(1)
M=1
DO 70 I=1,6
DO 70 L=1,20
IQ=LPP(L,I)
IF (IQ.LT.2) GO TO 70
M=M+1
YH=SMAX(M)
YL=SMIN(M)
IBEG=(M-1)*NREC+1
CALL KPLOT(GRAPH,STORE,STORE(IBEG),0,0,0,0,0,0)
1082 WRITE (KOUT,1082) TITLE(I), L
70 FORMAT (/,1H ,A8,I3)
CONTINUE
RETURN
END
```

```

SUBROUTINE KPLOT(W,X,Y,NTAPE,IX,IY,NVAR,Y1)

COMMON /PLOT1/
1 NV, NH, NCPW, LW, VLH(4), NXES, NDIR, IST, NGLV, NGLH, BSYM, GSYM,
2 PSYM, NDIM1, NDIM2, NO

DIMENSION W(1),X(1),Y(1),Y1(NVAR),STORE(70),Q(4),IPX(4),K(3)
EQUIVALENCE {Q(1),XL1},{Q(2),XH1},{(Q(3),YL1),(Q(4),YH1)}
EQUIVALENCE {ISC,K(1)},{JSC,K(3)}

DATA IPX/3,4,1,2/

C IF (NH.GT.121) NH=121
C NCPW IS THE NUMBER OF CHARACTERS PER WORD
C (60 BIT WORD 6 BIT DISPLAY CODE ON CDC)
C NCPW=10
LW=NH/NCPW+1
IF ((IST/10).GT.0) NCOUNT=0
NCOUNT=NCOUNT+1
IF (NCOUNT.EQ.10) IST=1
L=1
DO 10 I=1,4
Q(I)=-1.0E08*(-1)**I
K(L)=1
IF (VLH(L).EQ.VLH(L+1)) GO TO 10
K(L)=0
Q(I)=VLH(I)
IF {I.EQ.2} L=3
10 IF (NTAPE.EQ.0) GO TO 1200

C SKIP THIS PART IF PLOTTING FROM CORE
IFLAG=0
GO TO 40
1600 IFLAG=1
40 NN=0
REWIND NTAPE
READ (NTAPE) Y1
C GO TO 2800 ON EOF
IF (EOF(NTAPE))2800,100
100 NN=NN+1
IF (NN.LT.NDIM1) GO TO 50
IF (IFLAG.EQ.1) GO TO 1700
IF (ISC+JSC.EQ.0) GO TO 1710
300 NN=NN+1
IF (ISC.EQ.0) GO TO 600
XL1=AMIN1(XL1,Y1(IX))
XH1=AMAX1(XH1,Y1(IX))
IF (JSC.EQ.0) GO TO 200
600 YL1=AMIN1(YL1,Y1(IY))
YH1=AMAX1(YH1,Y1(IY))
200 READ (NTAPE) Y1
IF (EOF(NTAPE))1600,210
210 IF (NN-NDIM2) 300,300,1600

C RESUME HERE
1200 IF (ISC.EQ.0) GO TO 1400
DO 1300 I=NDIM1,NDIM2
XL1=AMIN1(XL1,X(I))
XH1=AMAX1(XH1,X(I))
IF (JSC.EQ.0) GO TO 1700
1400 DO 1500 I=NDIM1,NDIM2
YL1=AMIN1(YL1,Y(I))
YH1=AMAX1(YH1,Y(I))
1500 IF {ISC.EQ.1} CALL ADJUST(XH1,XL1)
1700 IF {JSC.EQ.1} CALL ADJUST(YH1,YL1)

```

```

1710    IF (NDIR/10) 1720,1740,1720
1720    TMP=XL1
      XL1=XH1
      XH1=TMP
1740    IF (NDIR-10*(NDIR/10)) 1760,1780,1760
1760    TMP=YL1
      YL1=YH1
      YH1=TMP
1780    J=7*(NCOUNT-1)+1
      IF (J.EQ.1) CALL QINIT(W)
      STORE(J)=PSYM
      DO 1800 I=1,4
      IF (NXES.EQ.0) L=I+J
      IF (NXES.GT.0) L=IPX(I)+J
1800    STORE(L)=Q(I)
      STORE(J+5)=(NH-1)/(STORE(J+2)-STORE(J+1))
      STORE(J+6)=(NV-1)/(STORE(J+4)-STORE(J+3))
2200    IF (NTAPE.EQ.0) GO TO 2500

C      SKIP THIS PART IF PLOTTING FROM CORE
DO 2400 I=NDIM1,NDIM2
IF (NXES.EQ.0) CALL KPLOTC(STORE(J),W,Y1(IX),Y1(IY))
IF (NXES.GT.0) CALL KPLOTC(STORE(J),W,Y1(IY),Y1(IX))
2400    READ (NTAPE) Y1
      IF (EOF(NTAPE)) 2800,2700

C      SKIP THIS PART IF PLOTTING FROM A FILE
2500    DO 2600 I=NDIM1,NDIM2
      IF (NXES.EQ.0) CALL KPLOTC(STORE(J),W,X(I),Y(I))
      IF (NXES.GT.0) CALL KPLOTC(STORE(J),W,Y(I),X(I))

C      RESUME HERE
2700    IF ((IST-10*(IST/10)).GT.0) CALL QPRINT(W,NO,NCOUNT,STORE)
      RETURN

C      ERROR MESSAGE
2800    WRITE (NO,2900)
2900    FORMAT(//32H INSUFFICIENT DATA ON INPUT FILE,/,1H ,28H PLOTTING ROUTINE TERMINATED)
      RETURN
      END
1

```

```
SUBROUTINE ADJUST(XH1,XL1)
IF (XH1.EQ.XL1) XL1=0.9*XL1-10.0
A=IFIX(100.0+ ALOG10(XH1-XL1))-100.0
XH1T=XH1*10.0**(1.0-A)
XL1T=XL1*10.0**(1.0-A)
IF (XH1T.GE. 0.0) XH1T=IFIX(XH1T+0.9)
XH1T=IFIX(XH1T)
IF (XL1T.LE. 0.0) XL1T=IFIX(XL1T-0.9)
XL1T=IFIX(XL1T)
XH1=XH1T*10.0**(A-1.0)
XL1=XL1T*10.0**(A-1.0)
RETURN
END
```

```
SUBROUTINE QINIT(IMAGE)

COMMON /PLOT1/
1 NV,NH,NCPW,LW,Q(4),NXES,NDIR,IST,NGLV,NGLH,BSYM,GSYM
DIMENSION IMAGE(1)
DATA IBLNK/10H

N=LW*NV
100 DO 100 I=1,N
      IMAGE(I)=IBLNK
      DO 101 I=1,NH
      CALL QPLOT(IMAGE,I,1,BSYM)
101   CALL QPLOT(IMAGE,I,NV,BSYM)
      DO 102 I=1,NV
      CALL QPLOT(IMAGE,1,I,BSYM)
102   CALL QPLOT(IMAGE,NH,I,BSYM)
1800   IF (NGLV.EQ.0) GO TO 2000
      NGLV1=NGLV+1
      NH1=NH-1
      DO 1900 I=NGLV1,NH1,NGLV
      DO 1900 J=1,NV
1900   CALL QPLOT(IMAGE,I,J,GSYM)
2000   IF (NGLH.EQ.0) RETURN
      NGLH1=NGLH+1
      NV1=NV-1
      DO 2100 I=NGLH1,NV1,NGLH
      DO 2100 J=1,NH
2100   CALL QPLOT(IMAGE,J,I,GSYM)
      RETURN
      END
```

```
SUBROUTINE KPLOTC(W,IMAGE,X,Y)
DIMENSION W(1), IMAGE(1)
COMMON /PLOT1/ NV, NH
J=(X-W(2))*W(6)+1.5
IF ((J.LE.0).OR.(J.GT.NH)) RETURN
I=NV-IFIX((Y-W(4))*W(7)+0.5)
IF ((I.LE.0).OR.(I.GT.NV)) RETURN
CALL QPLOT (IMAGE,J,I,W(1))
RETURN
END
```

```
SUBROUTINE QPLOT(IMAGE,J,I,SYM)
COMMON /PLOT1/ NV, NH, NCPW, LW
DIMENSION IMAGE(1)

II=J/NCPW
L=J-NCPW*II
II=II+1
IF (L) 101,101,102
101
L=NCPW
II=II-1
102
IW=II+(I-1)*LW
CALL PLACE(IMAGE(IW),L,SYM,1)
103
RETURN
END
```

C SUBROUTINE PLACE(A,N,B,M)  
C THE MTH CHAR OF B REPLACES  
C THE NTH CHARACTER OF A  
C CHAR POSITIONS ARE 1 TO 10 FROM LEFT TO RIGHT  
  
COMMON/INOU/KIN,KOUT  
INTEGER A, B, BX, BY  
DATA MASK/77B/  
  
C CHECK FOR VALID ARGUMENTS  
IF (N.GT.10 .OR. M.GT.10) GO TO 900  
IF (N.LT.1 .OR. M.LT.1) GO TO 900  
  
C NULL ALL BUT THE MTH CHAR OF B, PUT IT IN BX  
C NULL THE NTH CHAR OF A  
NSHFT=60-6\*N  
MSHFT=60-6\*M  
MASKBY = SHIFT(MASK,NSHFT)  
MASKB = SHIFT(MASK,MSHFT)  
MASKA = COMPL(MASKBY)  
A = AND(A,MASKA)  
BX = AND(B,MASKB)  
  
C SHIFT THE MTH CHAR OF BX TO THE NTH POSITION  
C PUT IT IN BY AND NULL ALL BUT THE NTH CHAR  
MNSHFT=6\*(M-N)  
BY = SHIFT(BX,MNSHFT)  
BY = AND(BY,MASKBY)  
  
C COMBINE A AND BY  
A = OR(A,BY)  
  
RETURN  
  
C N OR M OUT OF BOUNDS  
900 1900 1 WRITE (KOUT,1900)  
FORMAT (1H,20HERROR IN SUBR. PLACE,/,  
24H N OR M IS OUT OF BOUNDS)  
CALL EXIT  
  
END

```
SUBROUTINE QPRINT(IMAGE,NO,NCOUNT,STORE)
DIMENSION IMAGE(1), STORE(1)
COMMON /PLOT1/ NV, NH, NCPW, LW
CALL PAGEFD(NO,1)
DO 110 I=1,NCOUNT
IB=7*(I-1)+1
110 WRITE (NO,102) STORE(IB+1),STORE(IB),STORE(IB),STORE(IB+2)
NCANT=NV-NCOUNT
IA=1
DO 150 I=1,NV
IB=I*LW
IF (I.GT.NCOUNT) GO TO 120
IBASE=(I-1)*7+1
WRITE (NO,103) STORE(IBASE),STORE(IBASE+4),(IMAGE(J),J=IA,IB)
GO TO 150
120 IF (I.GT.NCANT) GO TO 130
WRITE (NO,105) (IMAGE(J),J=IA,IB)
GO TO 150
130 IBASE=(I-1-NCANT)*7+1
WRITE (NO,103) STORE(IBASE),STORE(IBASE+3),(IMAGE(J),J=IA,IB)
150 IA=IA+LW
102 FORMAT(1H ,11X,1PE10.3,1X,A1,77X,A1,1PE10.3)
103 FORMAT(1H ,A1,1PE9.2,1X,12A10,A1)
105 FORMAT(1H ,11X,12A10,A1)
RETURN
END
```

```
SUBROUTINE DSCRT(N,A,DEL,EA,EAINT,NT)
DIMENSION A(1),EA(1),EAINT(1),COEF(30)
      SETS EA=EXP(A*DEL),EAINT=INTEGRAL EA 0 TO DEL
C      COMMON/MMAIN1/NDIM,NDIM1
      NN=N*NDIM
      NTM1=NT-1
      COEF(NT)=1.
      DO 10 I=1,NTM1
      II=NT-I
      COEF(II)=DEL*COEF(II+1)/FLOAT(I)
C      NT MUST BE AT LEAST 3
      II=1
      DO 30 I=1,N
      DO 20 J=I,NN,NDIM
      EAINT(J)=A(J)*COEF(1)
      EAINT(II)=EAINT(II)+COEF(2)
      30   II=II+NDIM1
      DO 60 L=3,NT
      T1=COEF(L)
      CALL MMUL(A,EAINT,N,N,N,EA)
      IF(L.EQ.NT)GO TO 70
      II=1
      DO 60 I=1,N
      DO 50 J=I,NN,NDIM
      EAINT(J)=EA(J)
      EAINT(II)=EAINT(II)+T1
      60   II=II+NDIM1
      DO 80 II=1,NN,NDIM1
      EA(II)=EA(II)+T1
      80   CONTINUE
      RETURN
      END
```

```

SUBROUTINE GMINV(NR,NC,A,U,MR,MT)
DIMENSION A(1),U(1),S(30)
COMMON/MAIN1/ NDIM,NDIM1
COMMON/INOU/ KIN,KOUT
TOL=1.E-12
MR=NC
NRM1=NR-1
TOL1=1.E-20
JJ=1
DO 100 J=1,NC
FAC=DOT(NR,A(JJ),A(JJ))
JM1=J-1
JRM=JJ+NRM1
JCM=JJ+JM1
DO 20 I=JJ,JCM
20   U(I)=0.
U(JCM)=1.0
IF(J.EQ.1) GO TO 54
KK=1
DO 30 K=1,JM1
IF(S(K).EQ.1.0) GO TO 30
TEMP=-DOT(NR,A(JJ),A(KK))
CALL VADD(K,TEMP,U(JJ),U(KK))
30   KK=KK+NDIM
DO 50 L=1,2
KK=1
DO 50 K=1,JM1
IF(S(K).EQ.0.) GO TO 50
TEMP=-DOT(NR,A(JJ),A(KK))
CALL VADD(NR,TEMP,A(JJ),A(KK))
CALL VADD(K,TEMP,U(JJ),U(KK))
50   KK=KK+NDIM
TOL1=TOL*FAC
FAC=DOT(NR,A(JJ),A(JJ))
54   IF(FAC.GT.TOL1) GO TO 70
DO 55 I=JJ,JRM
55   A(I)=0.
S(J)=0.
KK=1
DO 65 K=1,JM1
IF(S(K).EQ.0.) GO TO 65
TEMP=-DOT(K,U(KK),U(JJ))
CALL VADD(NR,TEMP,A(JJ),A(KK))
65   KK=KK+NDIM
FAC=DOT(J,U(JJ),U(JJ))
MR=MR-1
GO TO 75
70   S(J)=1.0
KK=1
DO 72 K=1,JM1
IF(S(K).EQ.1.) GO TO 72
TEMP=-DOT(NR,A(JJ),A(KK))
CALL VADD(K,TEMP,U(JJ),U(KK))
72   KK=KK+NDIM
75   FAC=1./SQRT(FAC)
DO 80 I=JJ,JRM
80   A(I)=A(I)*FAC
DO 85 I=JJ,JCM
85   U(I)=U(I)*FAC
100  JJ=JJ+NDIM
IF(MR.EQ.NR.OR.MR.EQ.NC) GO TO 120
IF(MT.NE.0) WRITE(KOUT,110) NR,NC,MR
110  FORMAT(I3,1HX,I2,8H M RANK,I2)
120  NEND=NC*NDIM
JJ=1

```

```
DO 135 J=1,NC
DO 125 I=1,NR
II=I-J
S(I)=0.
125   DO 125 KK=JJ,NEND,NDIM
      S(I)=S(I)+A(II+KK)*U(KK)
      II=J
      DO 130 I=1,NR
      U(II)=S(I)
      II=II+NDIM
130   JJ=JJ+NDIM1
135   RETURN
      END
```

```
C      SUBROUTINE MAT2(N1,N2,X,Y,Z)
C      Z=XY' X,Y=N1*N2,Z=Z'
C      Z AND Y CAN BE EQUIVALENT
C      DIMENSION X(1),Y(1),Z(1)
C      COMMON/MAIN1/NDIM,NDIM1
C      NN2=N2*NDIM
C      II=1
C      DO 10 I=1,N1
C      IJ=II
C      DO 5 J=I,N1
C      Z(IJ)=DOT2(NN2,X(I),Y(J))
5       IJ=IJ+NDIM
C      J=II
C      IJ=J
3       IJ=IJ-NDIM
C      IF(IJ.LT.I) GO TO 10
C      J=J-1
C      Z(IJ)=Z(J)
C      GO TO 3
10      II=II+NDIM1
C      RETURN
C      END
```

```
C      SUBROUTINE MAT5A(X,Y,N1,N2,N3,Z)
          Z=XT*Y   X=N2*N1, Y=N2*N3
          DIMENSION X(1),Y(1),Z(1)
          COMMON/MAIN1/NDIM
          N1M1=N1-1
          NN3=N3*NDIM
          DO 1 I=1,NN3,NDIM
              II=I+N1M1
              DO 1 J=I,II
                  Z(J)=0.0
                  ENTRY MAT5AS
                  NN3=N3*NDIM
                  DO 10 K=1,N2
                      KK=K
                      DO 8 I=1,N1
                          C1=X(KK)
                          IF(C1.NE.0.0) CALL VADD1(NN3,C1,Z(I),Y(K))
                          KK=KK+NDIM
                  10 CONTINUE
                  RETURN
          END
```

```
C      SUBROUTINE MAT6(N1,N2,X,Y,Z)
C      Z=X*Y, WHERE X=N1*N2, Y=N1*N2, Z=Z'=N1*N1
C      DIMENSION X(1), Y(1), Z(1)
C      COMMON /MAIN1/ NDIM, NDIM1
C      NN1=N1*NDIM
C      DO 1 I=1,N1
C      DO 1 J=I,NN1,NDIM
C      Z(J)=0.0
1      CONTINUE
C      ENTRY MAT6S
C      Z=Z+X*Y
C      NN2=N2*NDIM
C      NN1=N1*NDIM
C      DO 6 K=1,NN2,NDIM
C      KK=K-1
C      J=1
C      DO 6 I=1,N1
C      C1=Y(I+KK)
C      IF (C1.NE.0.0) CALL VADD(I,C1,Z(J),X(K))
C      J=J+NDIM
6      CONTINUE
C      IF (N1.EQ.1) RETURN
C      NN2=NDIM1+1
C      DO 10 K=NN2,NN1,NDIM1
C      I=K
C      J=K
8      I=I-1
C      J=J-NDIM
C      Z(J)=Z(I)
C      IF (J.GT.NDIM) GO TO 8
C      CONTINUE
C      RETURN
10     END
```

```
SUBROUTINE MMUL(X,Y,N1,N2,N3,Z)
DIMENSION X(1),Y(1),Z(1)
COMMON/MAIN1/NDIM
N1M1=N1-1
NN3=N3*NDIM
DO 1 I=1,NN3,NDIM
II=I+N1M1
DO 1 J=I,II
Z(J)=0.0
ENTRY MMULS
NN3=N3*NDIM
KK=0
DO 10 K=1,N2
DO 8 I=1,N1
C1=X(I+KK)
IF(C1.NE.0.0) CALL VADD1(NN3,C1,Z(I),Y(K))
CONTINUE
KK=KK+NDIM
10 RETURN
END
```

8  
10

```
C      SUBROUTINE DIAG2(N,A,B,C1,C2)
C      A = C1*B + C2*I
C      A,B ARE N*N MATRICES; I IS N*N IDENTITY MATRIX
C      DIMENSION A(1), B(1)
C      COMMON /MAIN1/ NDIM, NDIM1
C      NN=N*NDIM
C      NM1=N-1
C      II=1
C      IF (C1 .EQ. 1.0) GO TO 10
C      DO 5 J=1,NN,NDIM
C          K=J+NM1
C          DO 4 I=J,K
C              A(I)=C1*B(I)
C              A(II)=A(II)+C2
C              II=II+NDIM1
C          RETURN
C      10 DO 7 J=1,NN,NDIM
C          K=J+NM1
C          DO 6 I=J,K
C              A(I)=B(I)
C              A(II)=A(II)+C2
C              II=II+NDIM1
C          RETURN
C      END
```

```
SUBROUTINE IDENT(N,A,C1)
DIMENSION A(1)
COMMON/MAIN1/NDIM,NDIM1
NN=N*NDIM
II=1
DO 1 I=1,N
DO 2 J=I,NN,NDIM
A(J)=0.0
A{II}=C1
II=II+NDIM1
1      RETURN
2      END
```

C SUBROUTINE EQUATE(A,B,NR,NC)  
C A=B  
C MATRIX EQUATE  
C DIMENSION A(1), B(1)  
C CALL MSCALE(A,B,NR,NC,1.0)  
C RETURN  
C END

```
C      SUBROUTINE MSCALE(A,B,NR,NC,C1)
C      A=C1*B
C      A AND B MAY BE EQUIVALENT
C      DIMENSION A(1), B(1)
C      COMMON /MAIN1/ NDIM
C      NN=NC*NDIM
C      IF (C1 .EQ. 1.0) GO TO 10
C      IF (C1 .EQ. 0.0) GO TO 20
C      IF (C1 .EQ. -1.) GO TO 30
C      DO 5 I=1, NR
C      DO 5 J=I, NN, NDIM
C      5   A(J)=C1*B(J)
C      RETURN
C      10  DO 15 I=1, NR
C      DO 15 J=I, NN, NDIM
C      15  A(J)=B(J)
C      RETURN
C      20  DO 25 I=1, NR
C      DO 25 J=I, NN, NDIM
C      25  A(J)=0.0
C      RETURN
C      30  DO 35 I=1, NR
C      DO 35 J=I, NN, NDIM
C      35  A(J)=-B(J)
C      RETURN
C      END
```

```
FUNCTION DOT(NR,A,B)
DOUBLE PRECISION DDT1, DBLE
DIMENSION A(1),B(1)
DDT1=0.0D0
IF (NR .LE. 0) GO TO 2
DO 1 I=1, NR
1      DDT1=DDT1+DBLE(A(I)*B(I))
DOT=DDT1
RETURN
END
```

```
FUNCTION DOT2(NN,A,B)
DOUBLE PRECISION DDT2, DBLE
DIMENSION A(1),B(1)
COMMON /MAIN1/ NDIM
DDT2=0.0D0
IF (NN .LE. 0) GO TO 2
DO 1 I=1,NN,NDIM
1   DDT2=DDT2+DBLE(A(I)*B(I))
   DOT2=DDT2
RETURN
END
```

1  
2

```
FUNCTION DOT3(N,A,B)
DOUBLE PRECISION DDT3, DBLE
DIMENSION A(1),B(1)
COMMON /MAIN1/ NDIM
DDT3=0.0D0
IF (N .LE. 0) GO TO 2
1  II=1
DO 1 I=1,N
      DDT3=DDT3+DBLE(A(II)*B(I))
      II=II+NDIM
2  DOT3=DDT3
RETURN
END
```

```
SUBROUTINE VADD(N,C1,A,B)
DIMENSION A(1),B(1)
DO 1 I=1,N
1    A(I)=A(I)+C1*B(I)
      RETURN
      END
```

```
SUBROUTINE VADD1(NN,C1,A,B)
DIMENSION A(1),B(1)
COMMON/MAIN1/NDIM
DO 1 I=1,NN,NDIM
1    A(I)=A(I)+C1*B(I)
      RETURN
      END
```

```
SUBROUTINE VSCALE(X,Y,N,C1)
DIMENSION X(1),Y(1)
L=0
IF(C1.EQ.1.0) GO TO 5
IF(C1.EQ.0.0) GO TO 8
IF(C1.EQ.-1.) GO TO 13
1   L=L+1
    X(L)=C1*Y(L)
    IF(L.LT.N) GO TO 1
    RETURN
5   L=L+1
    X(L)=Y(L)
    IF(L.LT.N) GO TO 5
    RETURN
8   L=L+1
    X(L)=0.0
    IF(L.LT.N) GO TO 8
    RETURN
13  L=L+1
    X(L)=-Y(L)
    IF(L.LT.N) GO TO 13
    RETURN
END
```

```
C      SUBROUTINE VMAT1(A,X,N1,N2,Y)
Y=AX
DIMENSION A(1),X(1),Y(1)
COMMON/MAIN1/NDIM
DO 1 I=1,N1
Y(I)=0.0
II=I
DO 1 J=1,N2
Y(I)=Y(I)+A(II)*X(J)
II=II+NDIM
1      RETURN
END
```

```
C      SUBROUTINE VMAT2(Z,A,X,N1,N2,Y)
C      Y=Z+AX
C      DIMENSION A(1),X(1),Z(1),Y(1)
C      COMMON/MAIN1/NDIM
C      DO 1 I=1,N1
C          Y(I)=Z(I)
C          II=I
C          DO 1 J=1,N2
C              Y(I)=Y(I)+A(II)*X(J)
C              II=II+NDIM
C      RETURN
C      END
```

```
FUNCTION XGAIN(TH,XM,XS)
DIMENSION A(5)
DATA A/.2258368,-.2521287,1.259695,-1.287822,.9406461/
IF (TH.GT.0.) GO TO 2
XGAIN=1.0
RETURN
2
Y=XM
NS=2
IF(XS.LT.1.0E-10)XS=1.0E-10
IF(Y.EQ.0.) NS=1
ANS=0.
RMS=XS**2+XM**2
DO 1 I=1,NS
Z=.707*(TH+Y)/XS
TEMP=EXP(-Z**2)
X=1./(1.+327591*ABS(Z))
P=X*((((A(5)*X+A(4))*X+A(3))*X+A(2))*X+A(1))*1.128379
ERF=1.-P*TEMP
IF (Z.LT.0.) ERF=-ERF
ANS=ANS+(RMS+TH*Y)*(1.-ERF)-XS*Y*TEMP*.7975
1
Y=-Y
XGAIN=ANS/RMS/FLOAT(NS)
IF(XGAIN.LT.1.E-6) XGAIN=1.E-6
RETURN
END
```

```
C      SUBROUTINE MATIO(X,NR,NC,IO)
C      BATCH ORIENTED MATRIX I/O
C      IO=1    INPUT ONLY
C      IO=2    INPUT AND OUTPUT
C      IO=3    OUTPUT ONLY
C      IO=4    PUNCH
C
C      DIMENSION X(1)
C      COMMON /MAIN1/ NDIM
C      COMMON /INOU/ KIN, KOUT, KPTR, KPUNCH
C
C      JEND=NC*NDIM
C      GO TO (5,5,20,40) IO
C
C*****INPUT
5       DO 10 I=1,NR
          READ (KIN,1000) (X(IJ), IJ=I,JEND,NDIM)
10      CONTINUE
          IF (IO .EQ. 1) RETURN
C*****OUTPUT
20      DO 30 I=1,NR
          WRITE (KOUT,2000) (X(IJ), IJ=I,JEND,NDIM)
30      CONTINUE
          RETURN
C*****PUNCH
40      DO 50 I=1,NR
          WRITE (KPUNCH,3000) (X(IJ),IJ=I,JEND,NDIM)
50      CONTINUE
          RETURN
1000     FORMAT (8E10.0)
2000     FORMAT (1H,1P10E13.3)
3000     FORMAT (1P8E10.3)
        END
```

```
C      SUBROUTINE VECTIO(X,N,IO)
C      BATCH ORIENTED VECTOR I/O
C      IO=1.  INPUT ONLY
C      IO=2  INPUT AND OUTPUT
C      IO=3  OUTPUT ONLY
C      IO=4  PUNCH
C
C      DIMENSION X(1)
C      COMMON /INOU/ KIN, KOUT, KPTR, KPUNCH
C
C      GO TO (10,10,20,40) IO
C
C*****INPUT
10      READ (KIN,1000) (X(I), I=1,N)
      IF (IO .EQ. 1) RETURN
C*****OUTPUT
20      WRITE (KOUT,2000) (X(I), I=1,N)
      RETURN
C*****PUNCH
40      WRITE (KPUNCH,3000) (X(I), I=1,N)
      RETURN
1000    FORMAT (8E10.0)
2000    FORMAT (1H,1P10E13.3)
3000    FORMAT (1P8E10.3)
      END
```

```
C      SUBROUTINE PAGEFD(KFIL,KOUNT)
      WRITES KOUNT FORMFEEDS (1 IN COL 1) ON FILE KFIL
100      ENTRY FORMFD
          IF (KOUNT.LE.0) RETURN
1000     DO 200 I=1,KOUNT
           WRITE (KFIL,1000)
           FORMAT (1H1)
200      CONTINUE
          RETURN
         END
```

```
C      SUBROUTINE DAYTIM(KFIL)
      WRITES THE DATE AND THE TIME ON FILE KFIL
10      CALL TIME(LTIME)
      CALL DATE(LDATE)
      WRITE (KFIL,1000) LDATE, LTIME
1000    FORMAT(1H ,A10,2X,A10)
      RETURN
      END
```

## DISTRIBUTION

No. of Copies	No. of Copies				
Assistant Secretary of Defense for Manpower and Reserve Affairs Department of Defense Washington, D.C. 20301	1	Chief Human Engineering Laboratory Detachment Attn: DRXHE-FA, Mr. Sorin Frankford Arsenal Philadelphia Pennsylvania 19137	1		
HQ DA DAPE-PBR, Mr. Barber Washington, D.C. 20310	1	Commander US Army Materiel Development and Readiness Command Attn: DRXAM-TL 5001 Eisenhower Avenue Alexandria, Virginia 22333	2	Chief Human Engineering Laboratory Detachment Attn: DRXHE-PTA, Mr. Carlock Picatinny Arsenal Dover, New Jersey 07801	1
Headquarters US Army Medical R&D Command Attn: Behavior Sciences Res Br. Main Navy Building Washington, D.C. 20315	1	Chief Human Engineering Laboratory Detachment Attn: DRXHE-RI, Mr. Galbavy Rock Island Arsenal Rock Island, Illinois 61201	1		
Director Walter Reed Army Institute of Research Walter Reed Army Medical Center Attn: Neuropsychiatry Division Washington, D.C. 20012	1	Chief Human Engineering Laboratory Detachment Attn: DRXHE-TA, Mr. J. Erickson US Army Tank-Automotive Research and Development Command Warren, Mississippi 48090	1		
OAD/E&LS ODDR&E, Pentagon, Room 3D129 Attn: LTC Henry L. Taylor Washington, D.C. 20310	1	Chief Human Engineering Laboratory Detachment Attn: DRXHE-ME, Mr. Antenucci, c/o DRXFB-T0 US Army Mobility Equipment Research and Development Command Fort Belvoir, Virginia 22060	1		
US Army Human Engineering Laboratory Representative Attn: DRXHE-AV, Dr. M. Hofmann Directorate for RD&E US Army Aviation Systems Command P. O. Box 209 St. Louis, Missouri 63166	1	US Army Research Office Attn: Information Processing Office Box CM, Duke Station Durham, North Carolina 27706	1		
Commander US Naval Weapons Laboratory Attn: Technical Library Dahlgren, Virginia 22448	1	Commander US Army Air Defense School Attn: ATSA-CTD-MO Fort Bliss, Texas 79916	1		
Commander US Naval Weapons Center Attn: Code 533, Technical Library China Lake, California 93555	1	Commander Rock Island Arsenal Attn: SARRI-LP-L, Technical Library Rock Island, Illinois 61201	1		
Director, Development Center US Marine Corps Development and Education Command Attn: Chairman, Air Operations Division Quantico, California 22134	1	Commander US Army Electronics Command Attn: DRSEL-PA-RH, Mr. Baron Fort Monmouth, New Jersey 07703	1		
HQ Rome Air Development Center Attn: TILD Griffiss Air Force Base New York 13440	1	Library US Army War College Carlisle Barracks Pennsylvania 17013	1		
Chief Human Engineering Laboratory Detachment Attn: DRXHE-AM, Mr. Miles US Army Systems Analysis Activity Aberdeen Proving Ground Maryland 21005	1	Director US Army Ballistic Research Laboratory Attn: DRXBR-EB Aberdeen Proving Ground Maryland 21005	1		

No. of Copies		No. of Copies
Army Research Institute Field Unit Attn: Dr. Robert W. Bauer Building 2423 Fort Knox, Kentucky 40121	1	Director US Army Human Engineering Laboratory Attn: DRXHE-DBD Aberdeen Proving Ground Maryland 21005
Department of Transportation Library Reference and Research Branch, TAD-494.6 800 Independence Avenue SW Washington, D.C. 20591	1	Medical Library, Building 148 Naval Submarine Medical Research Laboratory Box 900, Submarine Base New London Croton, Connecticut 06340
US Postal Service Laboratory Attn: Mr. D.Y. Cornog Chief, HF Group 11711 Parklawn Drive Rockville, Maryland 20852	1	Code 455 Office of Naval Research Washington, D.C. 20360
Mr. Edgar M. Johnson US Army Research Institute Room 239, The Commonwealth Building 1320 Wilson Boulevard Arlington, Virginia 22209	1	Dr. Marshall J. Farr Associate Director, Personnel and Training Code 458 Office of Naval Research Washington, D.C. 20360
Federal Aviation Administration Civil Aeromedical Institute Library AC-101.1, P. O. Box 25082 Oklahoma City, Oklahoma 73125	1	Commandant US Army Artillery and Missile School Attn: USAAMS Technical Library Fort Sill, Oklahoma 73503
Department of Operations Analysis Naval Postgraduate School Attn: Professor James K. Arima Monterey, California 93940	1	ARI Field Unit P. O. Box 6057 Fort Bliss, Texas 79916
Commander USAVSCOM Attn: DRSAV-R-F, Mr. S. Moreland P. O. Box 209 St. Louis, Missouri 63166	1	Commander Fort Huachuca Support Command, US Army Attn: Tech References Division Fort Huachuca, Arizona 85613
Director Naval Research Laboratory Attn: Code 5132A Washington, D.C. 20390	1	Commander Attn: Technical Library White Sands Missile Range New Mexico 88002
Commanding Officer Naval Training Equipment Center Attn: Technical Library Orlando, Florida 32813	1	Director USA Air Mobility Research and Development Laboratory Attn: Dr. Richard S. Dunn Ames Research Center Moffett Field, California 94035
6J70 AMRL Attn: MRHE MRHE, Dr. M. J. Warrick MRHER, Mr. C. Bates, Jr. Wright-Patterson Air Force Base Ohio 45433	2 1 1	Commander US Army Electronics Command Attn: DRSEL-VL-E Fort Monmouth, New Jersey 07703
AF Flight Dynamics Laboratory Attn: FDCR (CDIC) AFFDC-FCR, LT Creg Peters Wright-Patterson Air Force Base Ohio 45433	1 1	Director Military Psychology and Leadership United States Military Academy West Point, New York 10996
		Commander Watervliet Arsenal Attn: SWEWV-RDT Watervliet, New York 12189
		Commander Frankford Arsenal Attn: Library (C2500, Building 51-2) Philadelphia, Pennsylvania 19137

	No. of Copies		No. of Copies
ARI Field Unit Attn: Library Fort Knox, Kentucky 40121	1	US Army Infantry School Library Infantry Hall Fort Benning, Georgia 31905	1
Commander US Army Tank-Automotive Command Attn: DRSTA-RHFL, Research Library Warren, Mississippi 48090	1	Project Manager Office of the Project Manager for Training Devices Attn: DRCPM-TND, Dr. R.E. Odom Fort Benning, Georgia 31905	1
Commander US Army Tank-Automotive Command Attn: DRSTA-R Warren, Mississippi 48090	1	Defense Documentation Center Cameron Station Alexandria, Virginia 22314	12
Director of Graduate Studies and Research Attn: Behavioral Sciences Representative US Army Command and General Staff College Fort Leavenworth, Kansas 66027	1	Commander US Army Materiel and Readiness Command Attn: DRCRD DRCDL 5001 Eisenhower Avenue Alexandria, Virginia 22333	1 1
US Army Agency for Aviation Safety Attn: Librarian Fort Rucker, Alabama 36360	1	Bolt, Beranek and Newman Inc. Attn: Dr. S. Baron Dr. D. Kleinmas Dr. J. Baliser 50 Moulton Street Cambridge, Maryland 02138	2 1 1
Chief Army Research Institute P. O. Box 476 Fort Rucker, Alabama 36360	1	DRXHE-MI, Mr. Chaikin	1
Commander US Army Aeromedical Research Laboratory P. O. Box 577 Attn: Dr. Kent Kimball Library Fort Rucker, Alabama 36360	1 1	DRCFM-HFE -AH -MPE -LDE -ROL-E -RK -HEL-T -TOE -MW	1 1 1 1 1 1 1 1
US Army Natick Research and Development Command Attn: Tech Library (DRXNM-STL) Natick, Massachusetts 01760	1	DRSMI-LP, Mr. Voigt -W	1 1
US Army Natick Research and Development Command Behavioral Sciences Division Attn: DRXNM-PRB DRXNM-PRBE Natick, Massachusetts 01760	1	DRDMI-X, Dr. McDaniel -T, Dr. Kobler -H -Y -YD -YT -TD -TDC -TDD -TDF -TDK -TDR -TDS -TDW -TDW, Mr. Dickson -TE -TG -TL -TPN, L. Aymett -TBD -TI (Record Set) (Reference Copy)	1 3 1 1
US Army Medical Bioengineering Research and Development Laboratory Fort Detrick, Building 568 Frederick, Maryland 21701	1		
Commander US Army Training Device Agency, Naval Training Equipment Center Attn: Code N2A Orlando, Florida 32813	1		